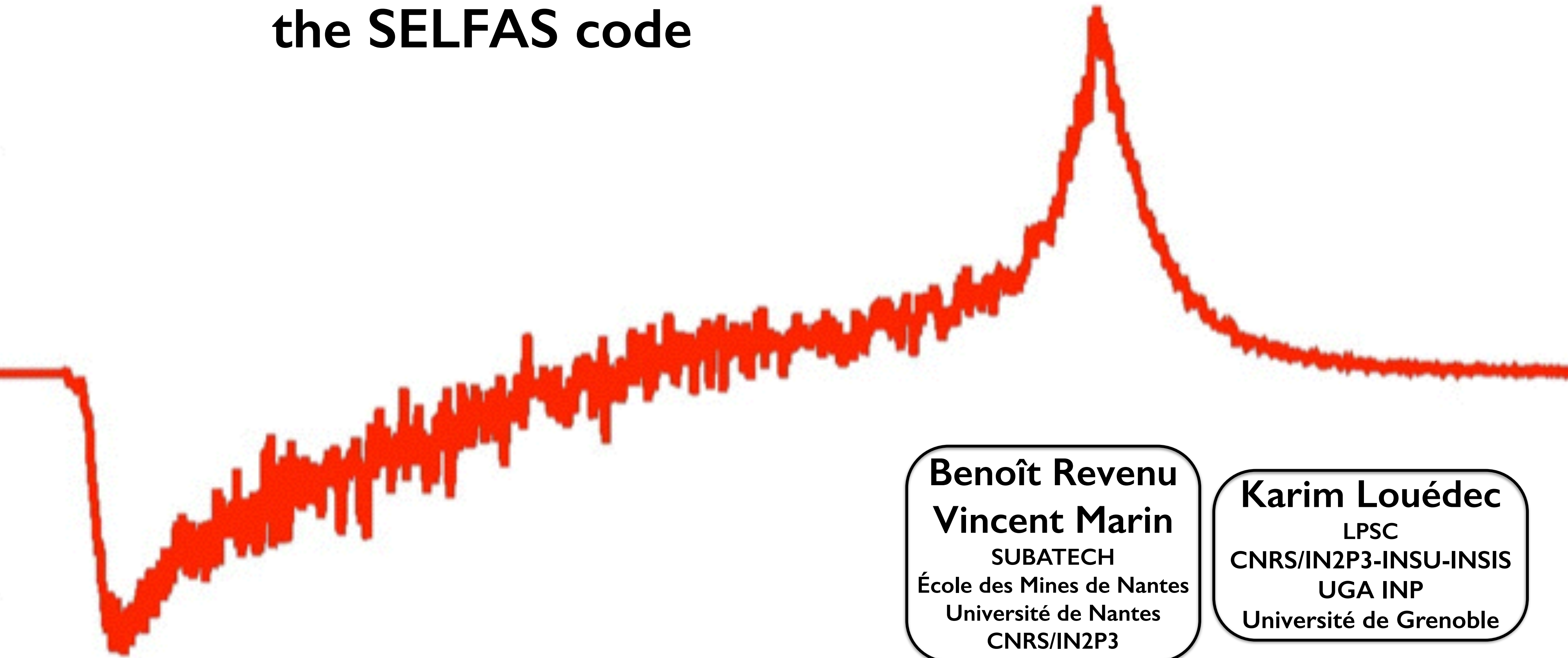


# Characterisation of the radio signal emission using the SELFAS code



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**Vincent Marin**  
SUBATECH  
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Université de Nantes  
CNRS/IN2P3

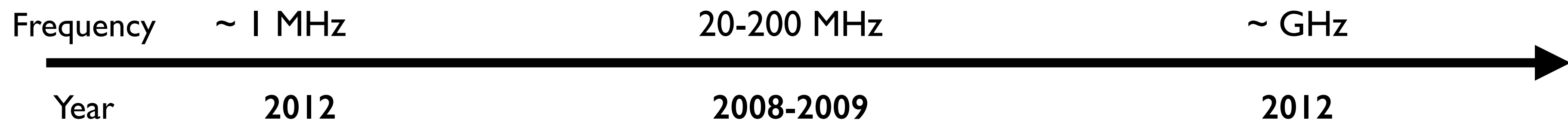
**Karim Louédec**  
LPSC  
CNRS/IN2P3-INSU-INSIS  
UGA INP  
Université de Grenoble

# Basics

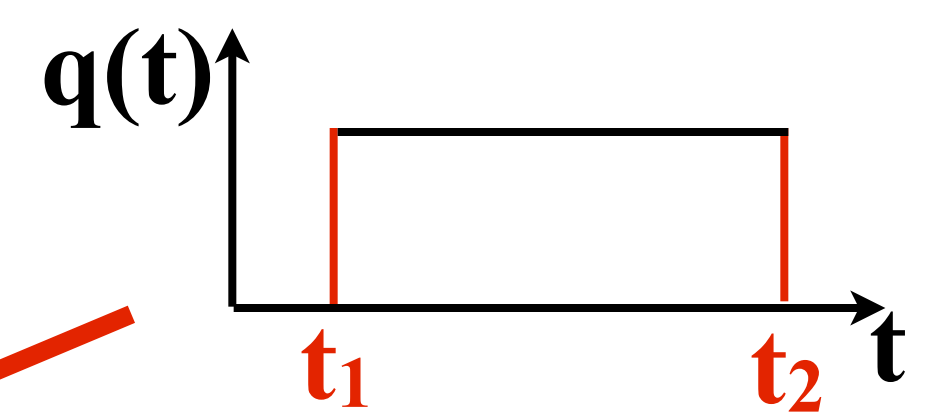
SELFAS computes the electric field emitted by the secondary  $e^+/e^-$  in EAS,

- in a large frequency band (kHz-GHz)
- no full shower simulation needed: based on shower universality concept
  - Longitudinal profile from GIL or CONEX
  - Energy distribution
  - Vertical and horizontal momentum direction
  - lateral distribution
  - Delay time (shower front thickness)
- track all  $e^+/e^-$  along their trajectory and sum up all individual contributions to the observer's location

Lafèbre et al  
*Astropart. Phys.*, 31(3):243 2009



# Formalism



For a single particle of charge  $q$  and a finite lifetime

Charge density  $\rho(\mathbf{x}', t') = q[\theta(t' - t_1) - \theta(t' - t_2)]\delta^3(\mathbf{x}' - \mathbf{x}_0(t'))$

Current density  $\mathbf{J}(\mathbf{x}', t') = \rho(\mathbf{x}', t')\mathbf{v}(t')$

Maxwell equation in Lorentz gauge:

$$\vec{E}(\vec{x}, t) = \frac{1}{4\pi\epsilon_0} \int d^3x' d^3t' \frac{1}{R} \left( -\nabla' \rho - \frac{1}{c^2} \frac{\partial \mathbf{J}}{\partial t'} \right)_{\text{ret}} \delta \left( t' - \left( t - \frac{|\mathbf{x} - \mathbf{x}'|}{c/\eta} \right) \right)$$

$$\vec{E}(\vec{x}, t) = \frac{1}{4\pi\epsilon_0} \left( \frac{q \vec{n}}{R^2(1 - \eta \vec{\beta} \cdot \vec{n})} + \frac{1}{c} \frac{\partial}{\partial t} \frac{q \vec{n}}{R(1 - \eta \vec{\beta} \cdot \vec{n})} - \frac{1}{c} \frac{\partial}{\partial t} \frac{q \vec{\beta}}{R(1 - \eta \vec{\beta} \cdot \vec{n})} \right)_{\text{ret}}$$

# Shower generation

Input : shower + site configuration  
+ antennas location + number of particles



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**Generation of the longitudinal profile**  
Following GIL parameterization (Greisen-Iljina-Linsley)  
or  
Using CONEX 2r4.37 (QGSJET-II.04, EPOS — ...)

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**Particle n : random depth X following the longitudinal profile**

**Initial  
conditions**

Lafèbre et al  
Astropart. Phys., 31(3):243, 2009

- Energy distribution
- Angular distribution
- Lateral distribution
- Delay time distribution

} Monte-Carlo

**Air refractive index**

$$\eta_i(h) = 1 + (\eta_{h=0} - 1) \frac{\rho_{air}(h)}{\rho_{air}(h=0)}$$
$$\eta_{h=0} = 1.000292$$

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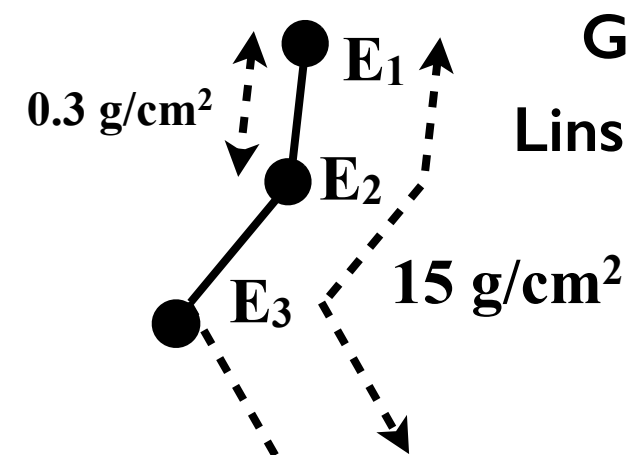
**Initial conditions**

Lafèbre et al  
Astropart. Phys., 31(3):243, 2009

- Energy distribution
- Angular distribution
- Lateral distribution
- Delay time distribution

Monte-Carlo

## Particle propagation and field calculation



Geomagnetic deviations + scattering deviations  
Linsley parameterization of US standard atmosphere

Compute field every 0.3 g/cm<sup>2</sup>  
along particle trajectory

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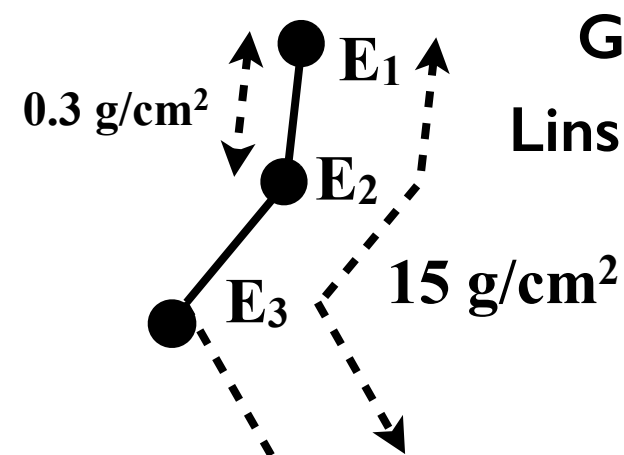
Initial  
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Lafèbre et al  
Astropart. Phys., 31(3):243, 2009

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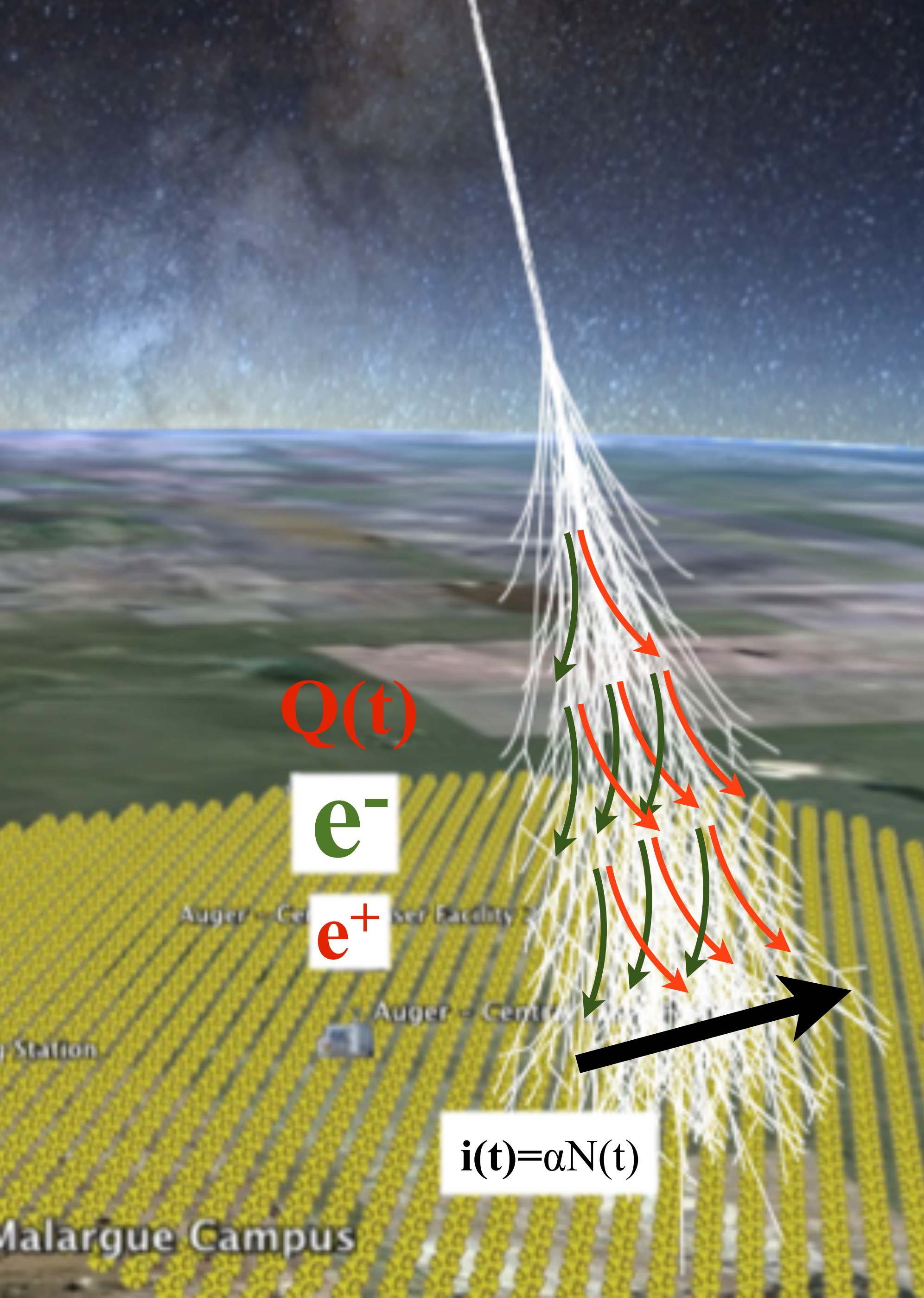
$$\eta_i(h) = 1 + (\eta_{h=0} - 1) \frac{\rho_{air}(h)}{\rho_{air}(h=0)}$$

$$\eta_{h=0} = 1.000292$$

Particle n+1



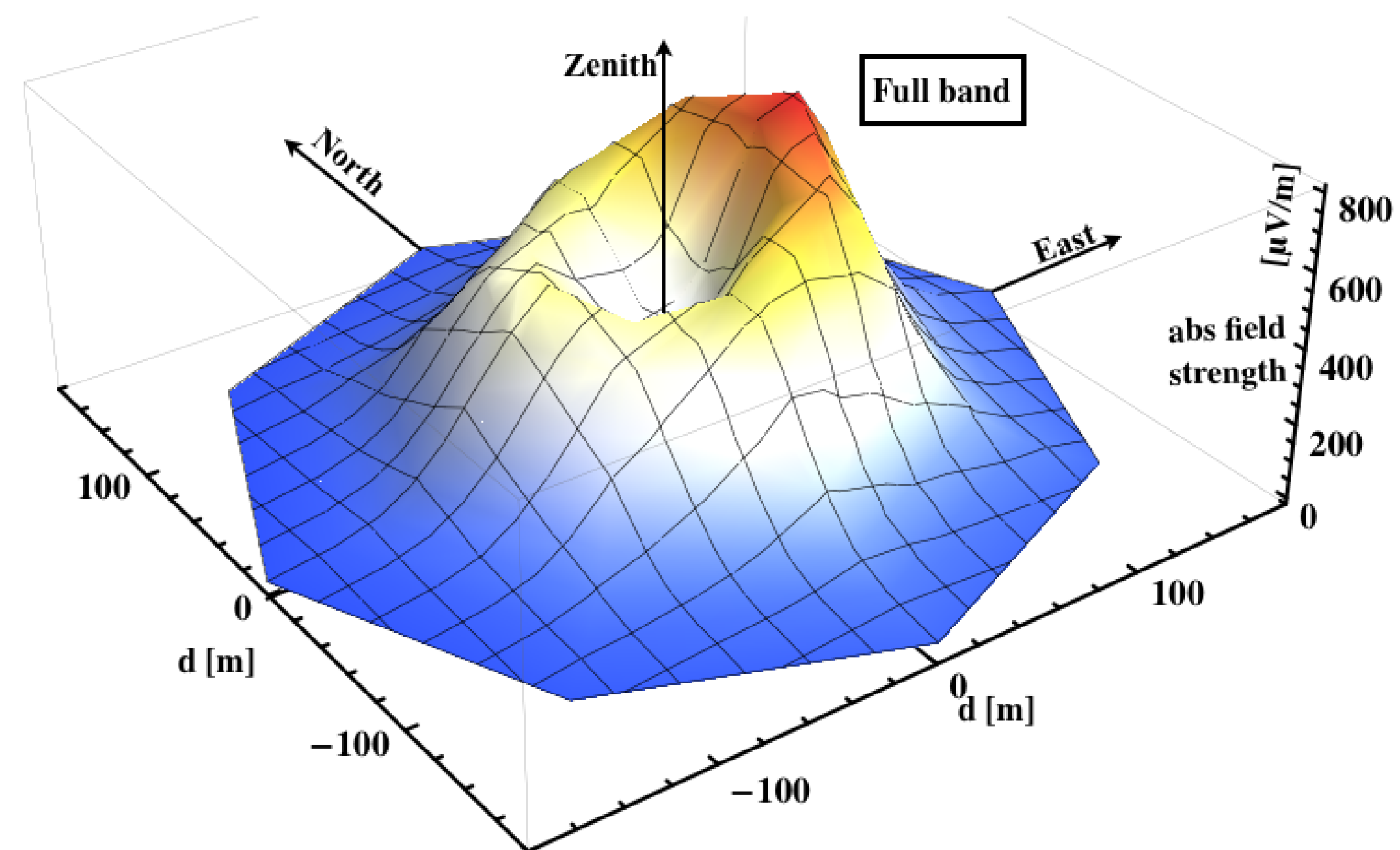
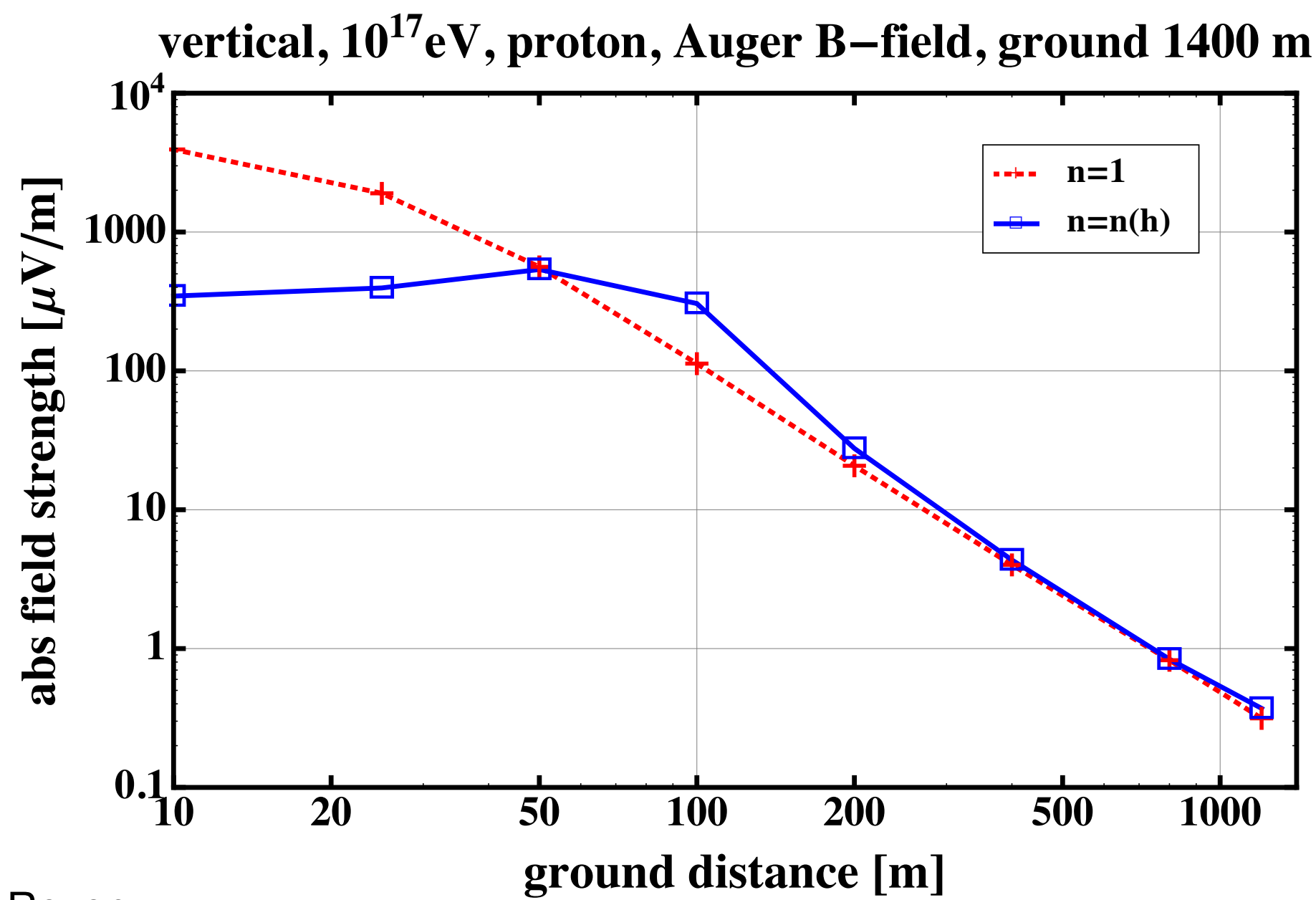
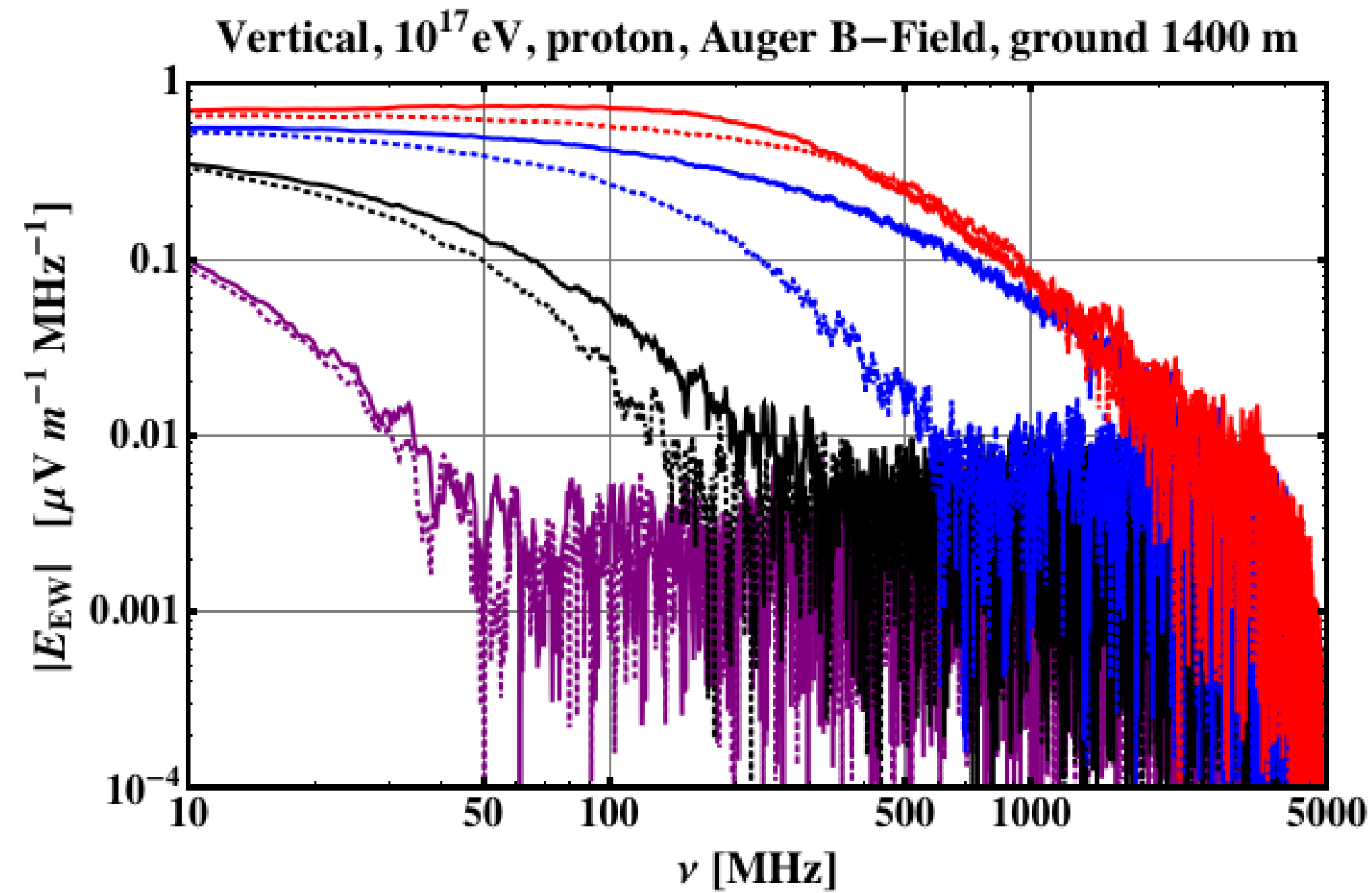
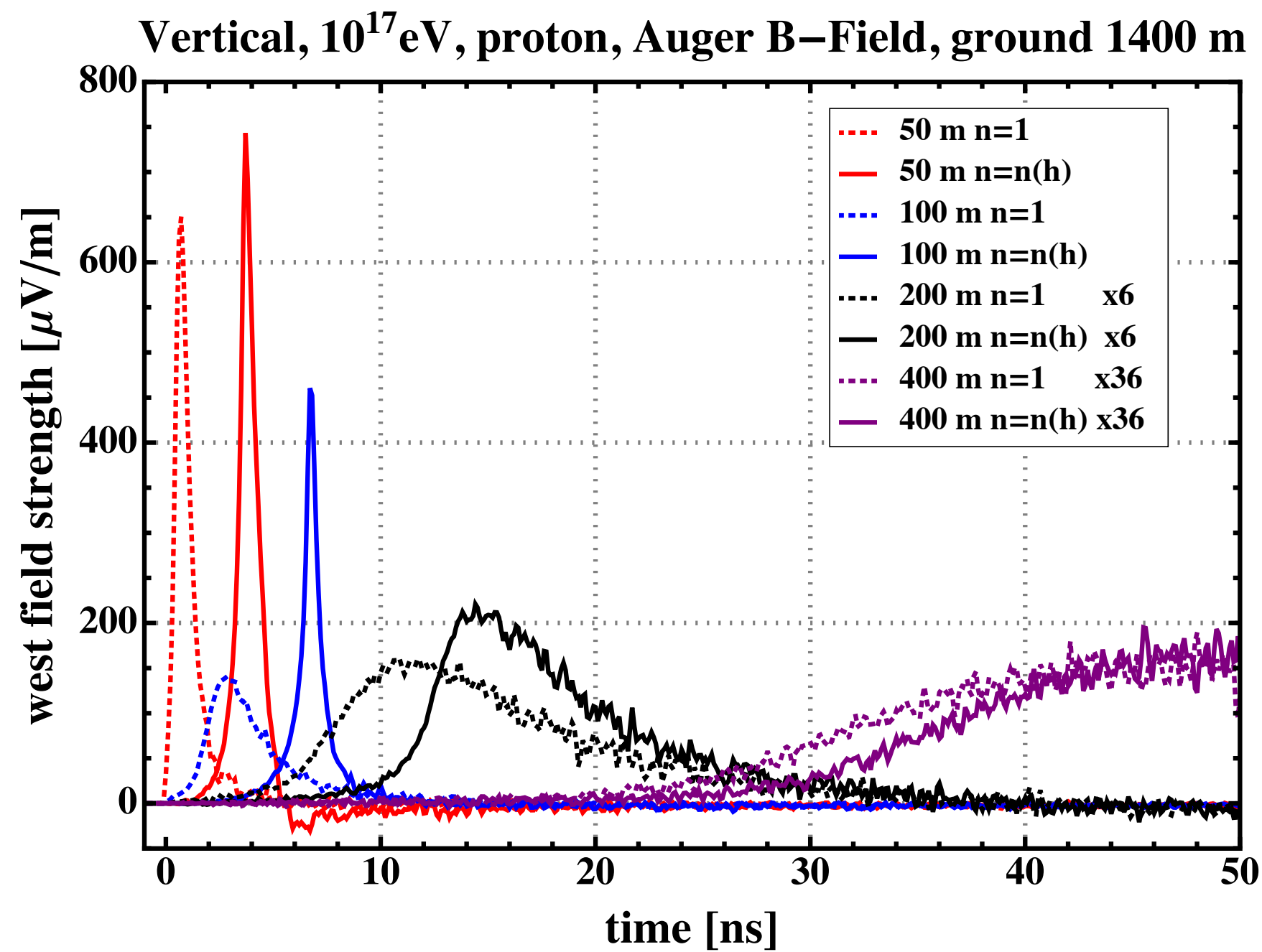
# Shower generation



$$\vec{E}(\vec{x}, t) = \frac{1}{4\pi\epsilon_0} \left( \sum_{i=1}^N \frac{q_i \vec{n}_i}{R_i^2 (1 - \eta \vec{\beta}_i \cdot \vec{n}_i)} + \frac{1}{c} \frac{\partial}{\partial t} \sum_{i=1}^N \frac{q_i \vec{n}_i}{R_i (1 - \eta \vec{\beta}_i \cdot \vec{n}_i)} - \frac{1}{c} \frac{\partial}{\partial t} \sum_{i=1}^N \frac{q_i \vec{\beta}_i}{R_i (1 - \eta \vec{\beta}_i \cdot \vec{n}_i)} \right)$$

Coulombian contribution  
 Charge excess contribution  
 Transverse current contribution





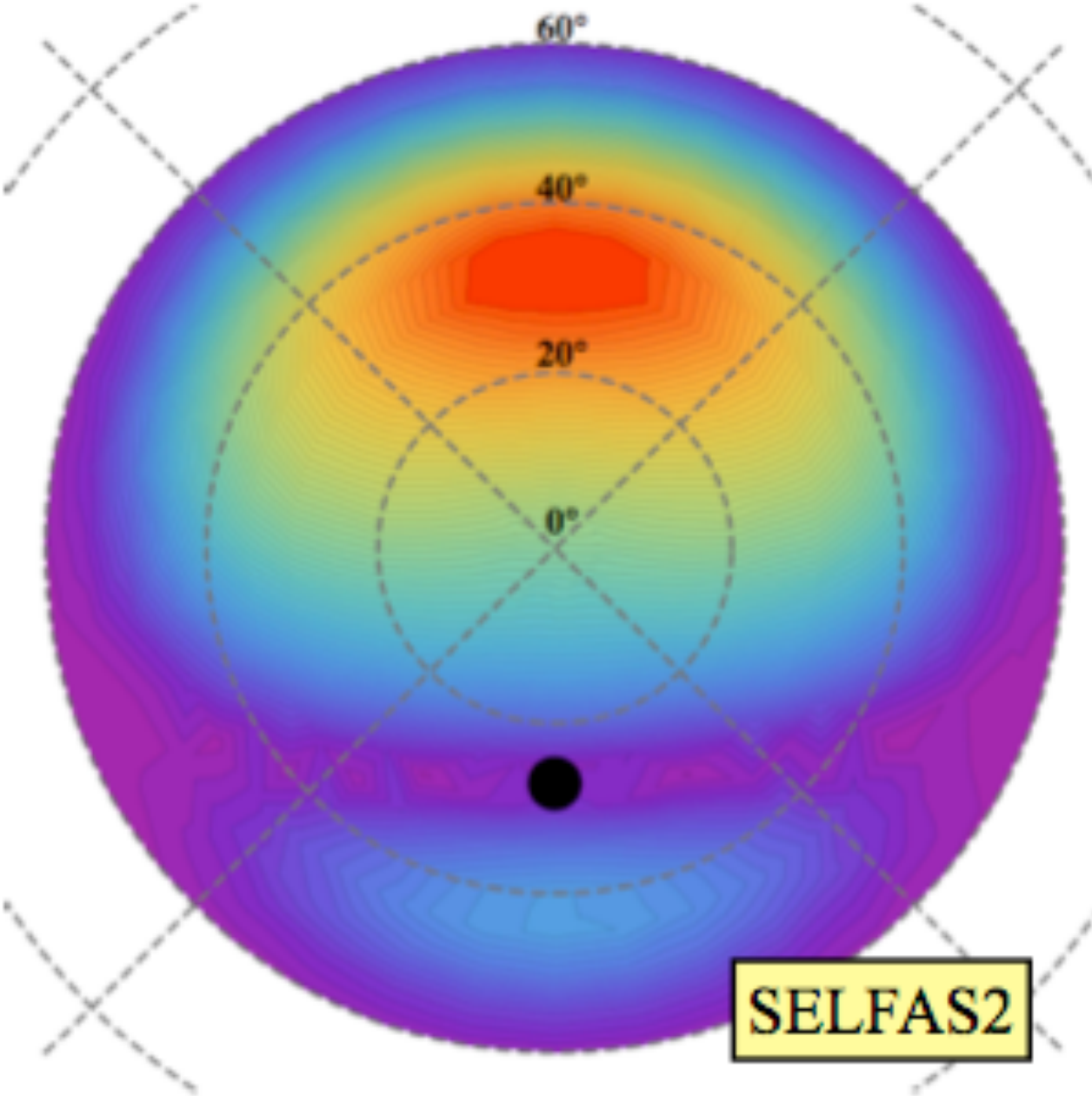


Transverse current contribution

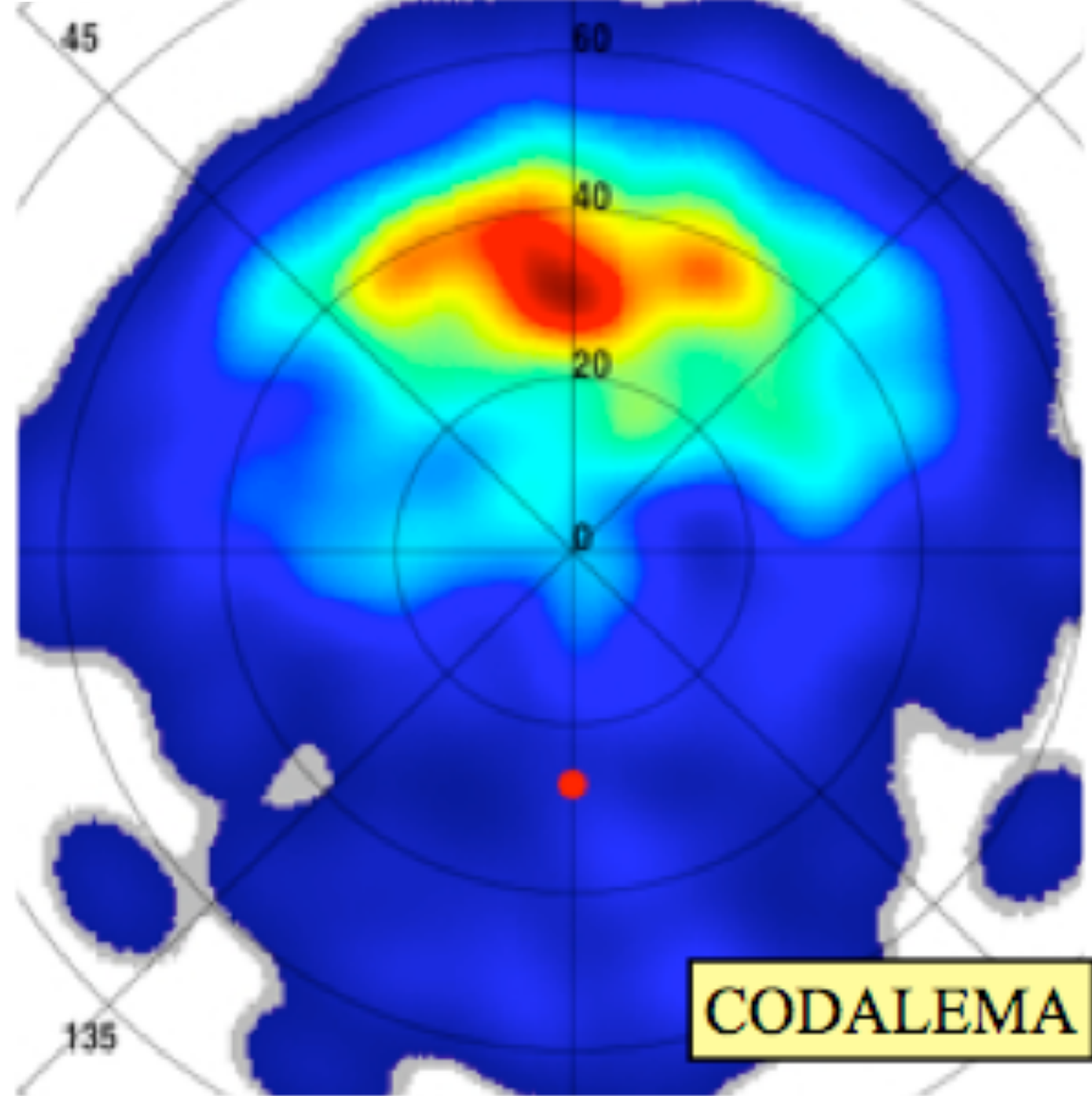
$$-\frac{1}{c} \frac{\partial}{\partial t} \sum_{i=1}^N \frac{q_i \vec{\beta}_i}{R_i (1 - \eta \vec{\beta}_i \cdot \vec{n}_i)}$$

dominant contribution!

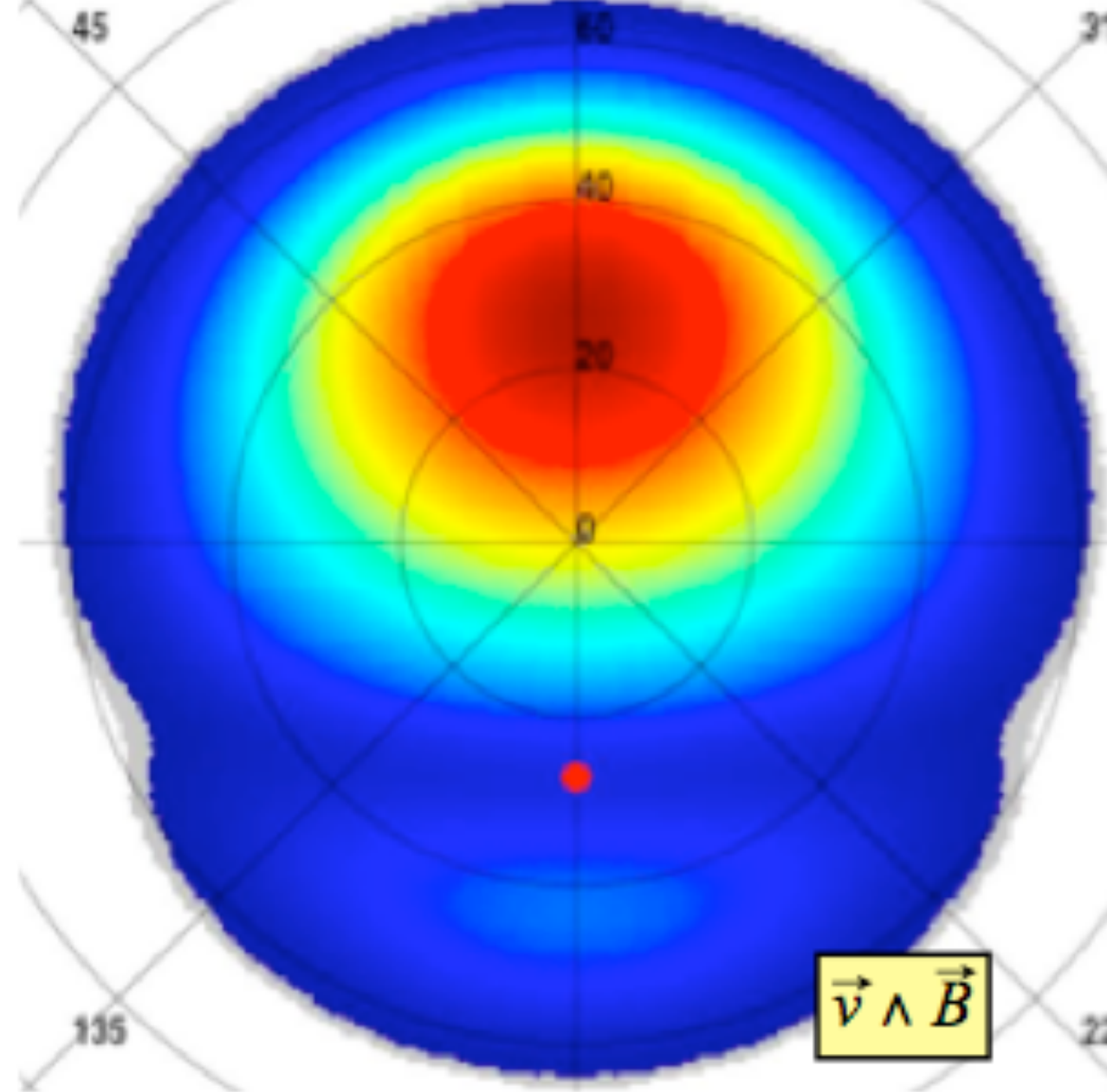
SELFAS



CODALEMA

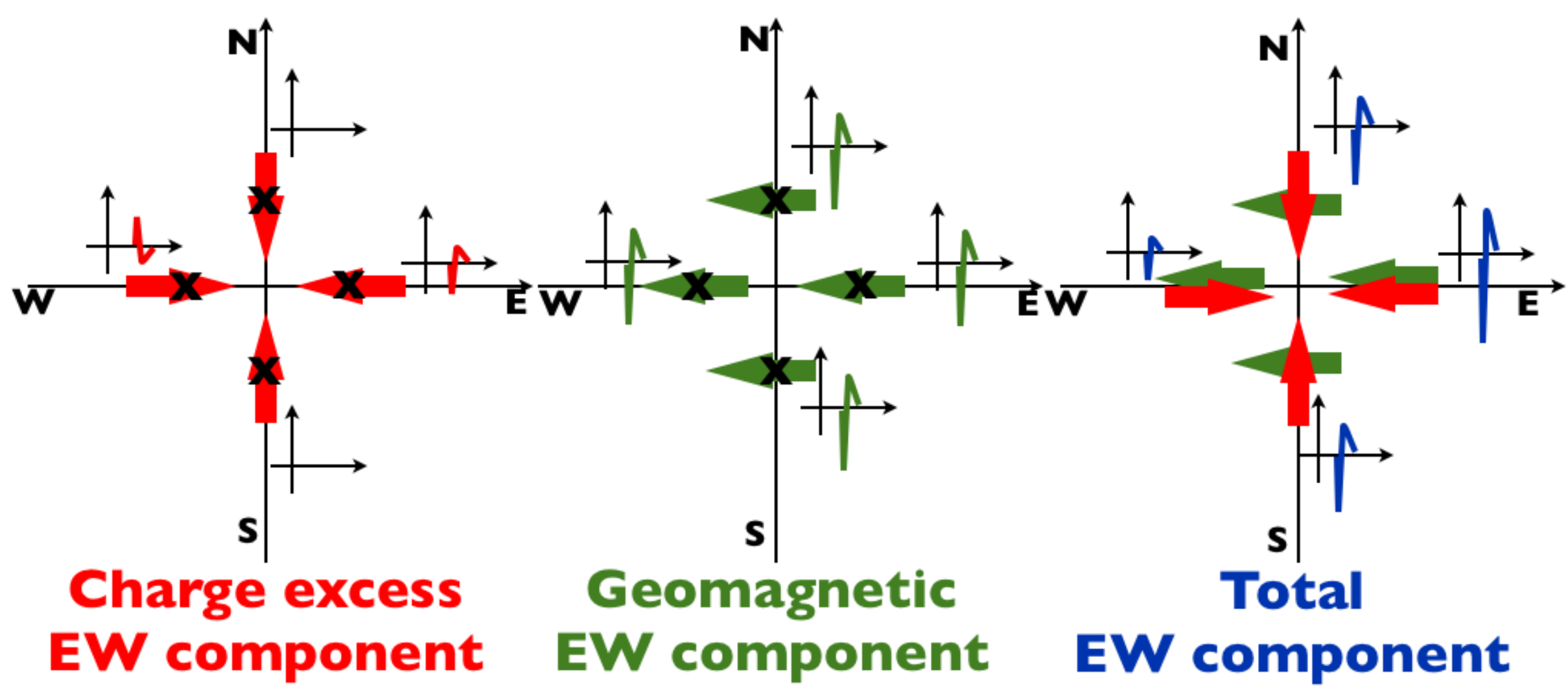


$\vec{v} \wedge \vec{B}$  EO

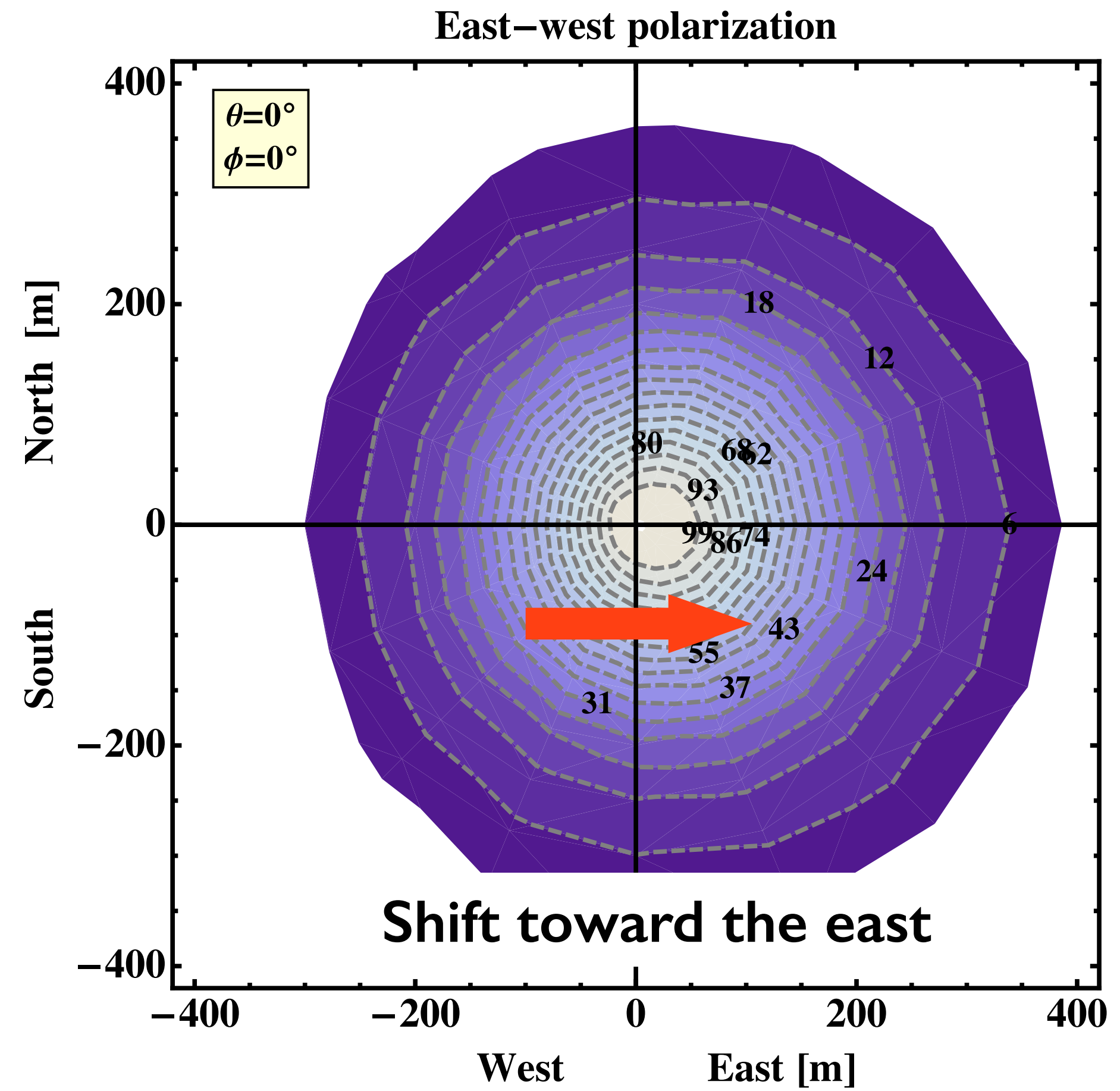


Charge excess contribution

$$+ \frac{1}{c} \frac{\partial}{\partial t} \sum_{i=1}^N \frac{q_i \vec{n}_i}{R_i (1 - \eta \vec{\beta}_i \cdot \vec{n}_i)}$$



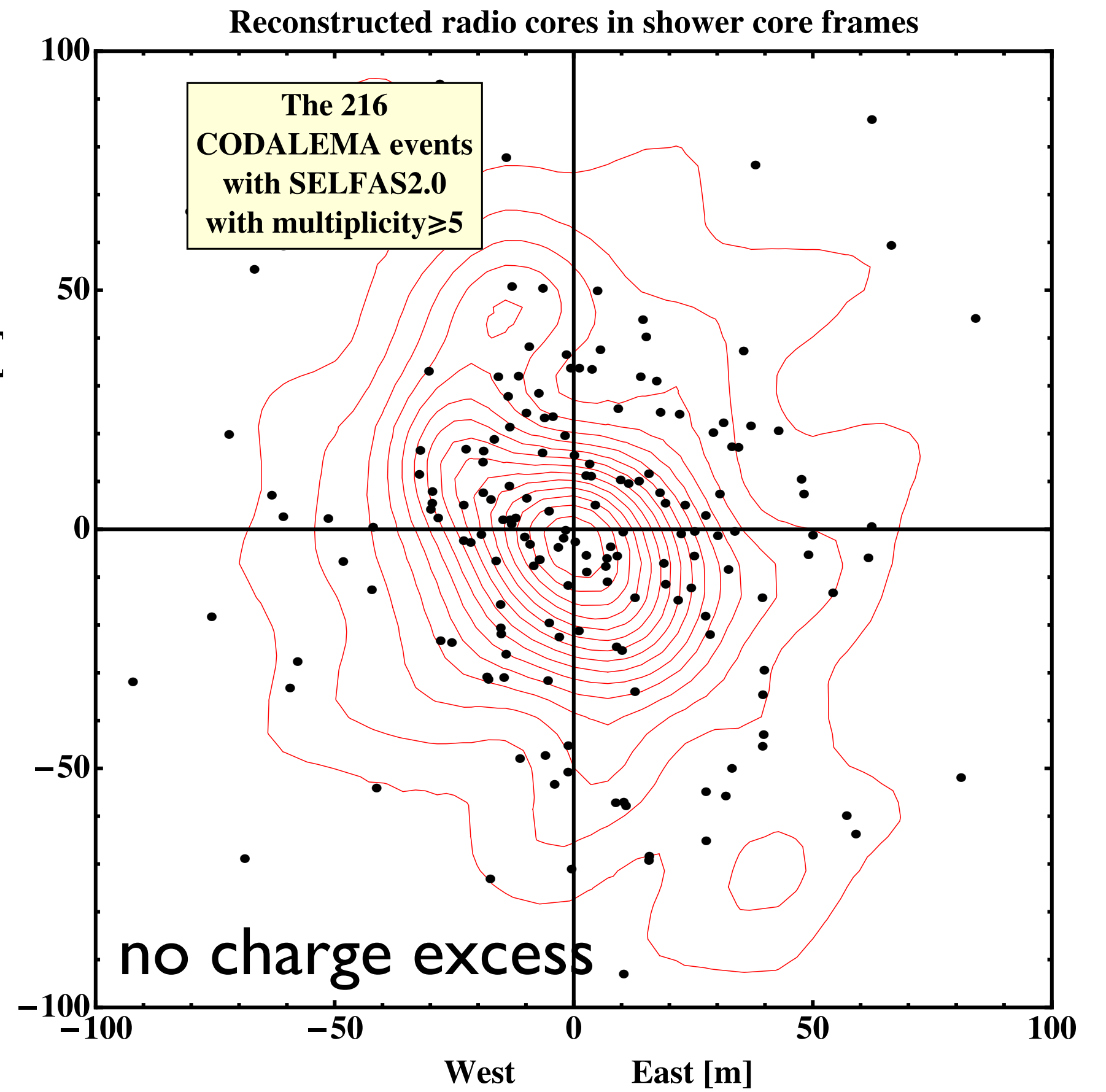
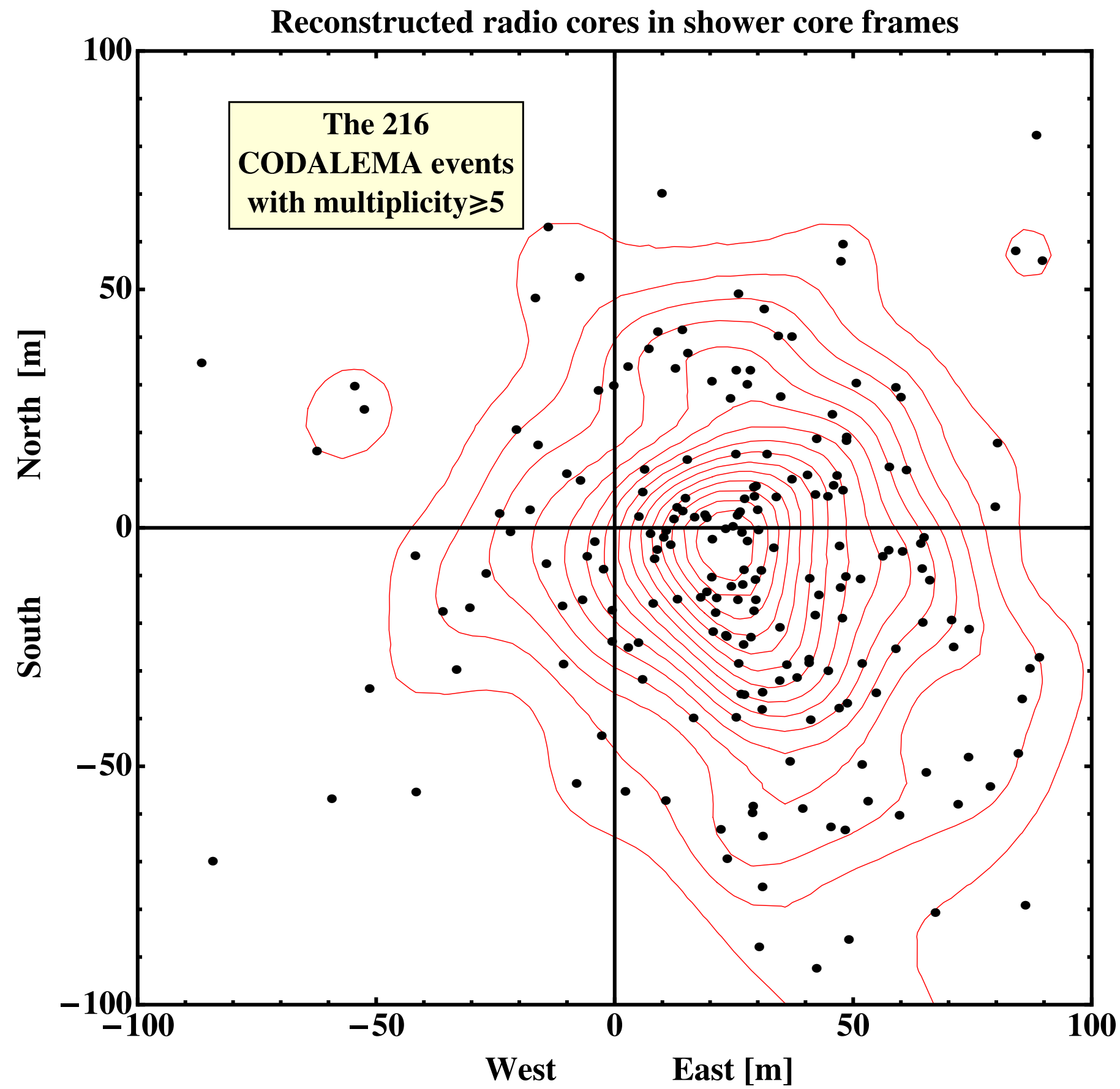
(+R-analysis, a-analysis by Tim this morning)





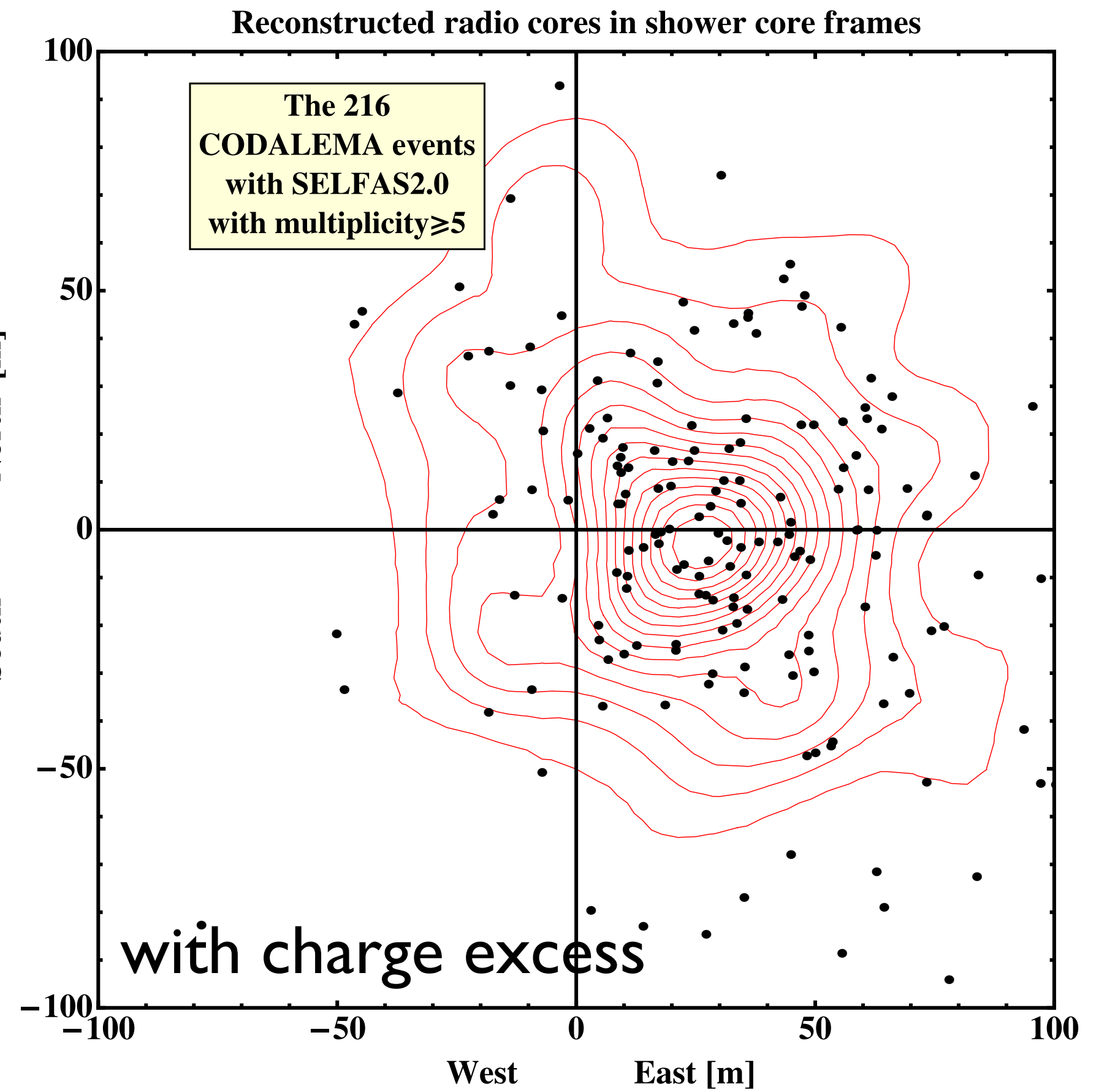
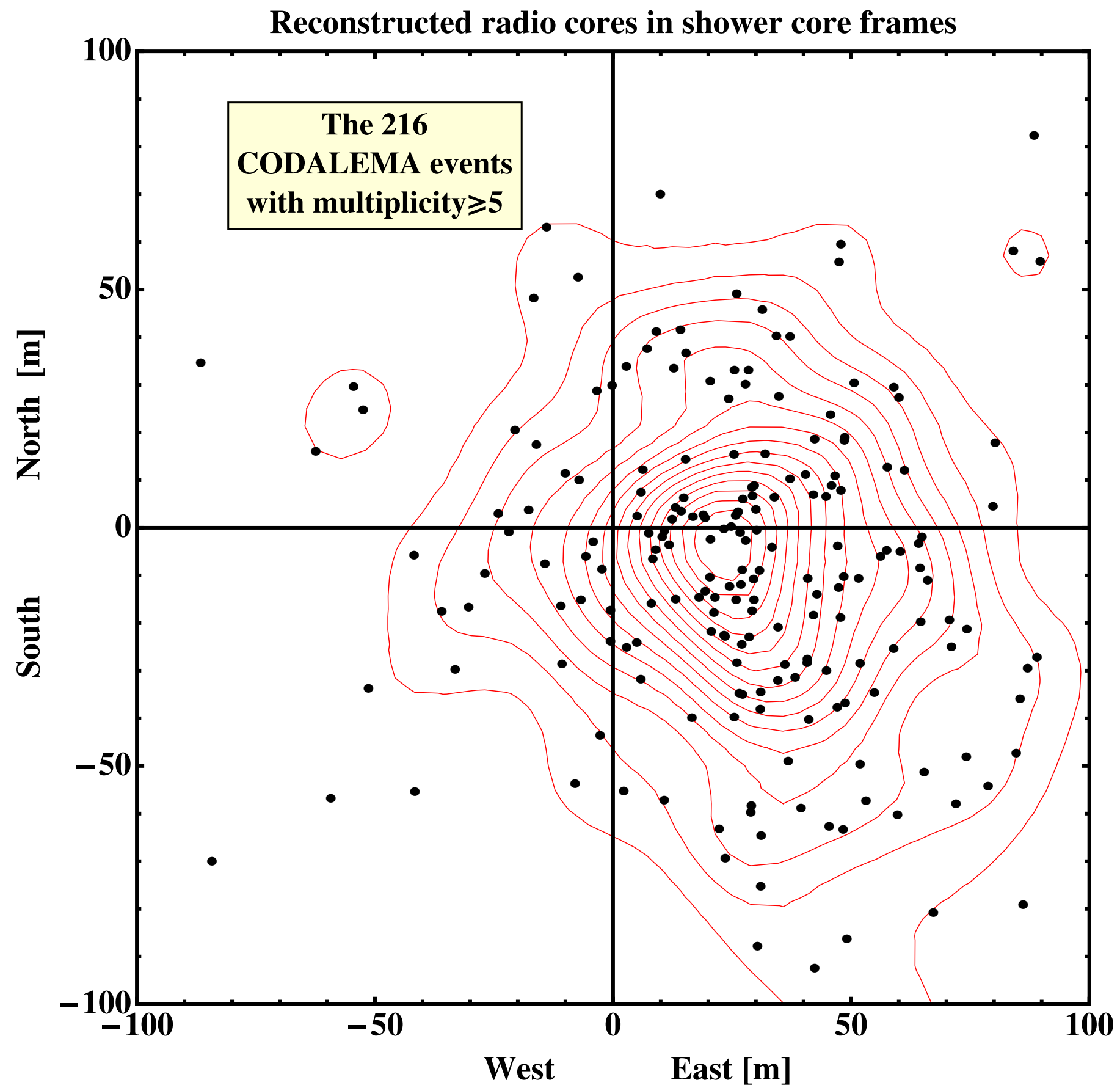
Charge excess contribution

$$+ \frac{1}{c} \frac{\partial}{\partial t} \sum_{i=1}^N \frac{q_i \vec{n}_i}{R_i (1 - \eta \vec{\beta}_i \cdot \vec{n}_i)}$$



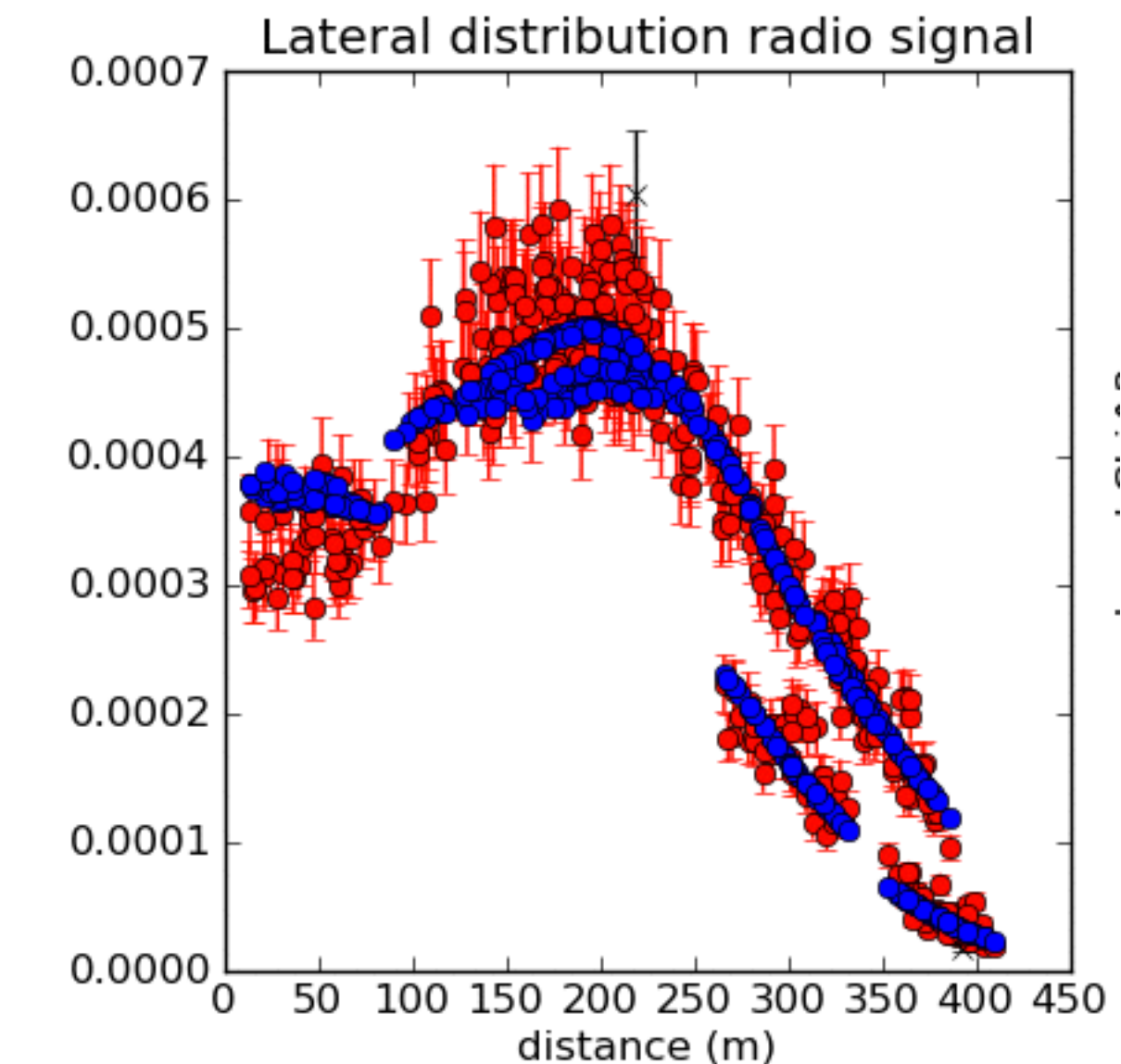
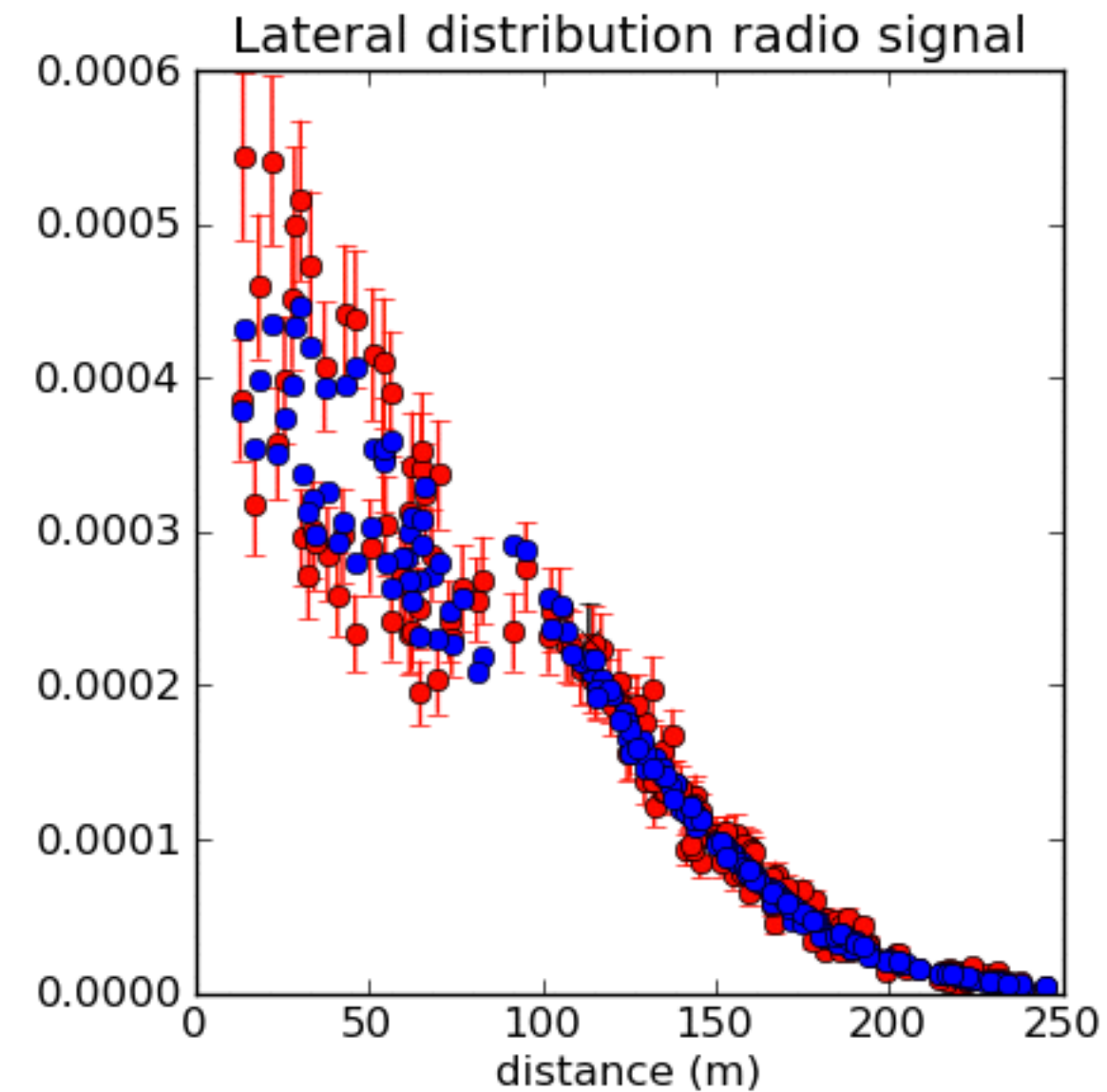
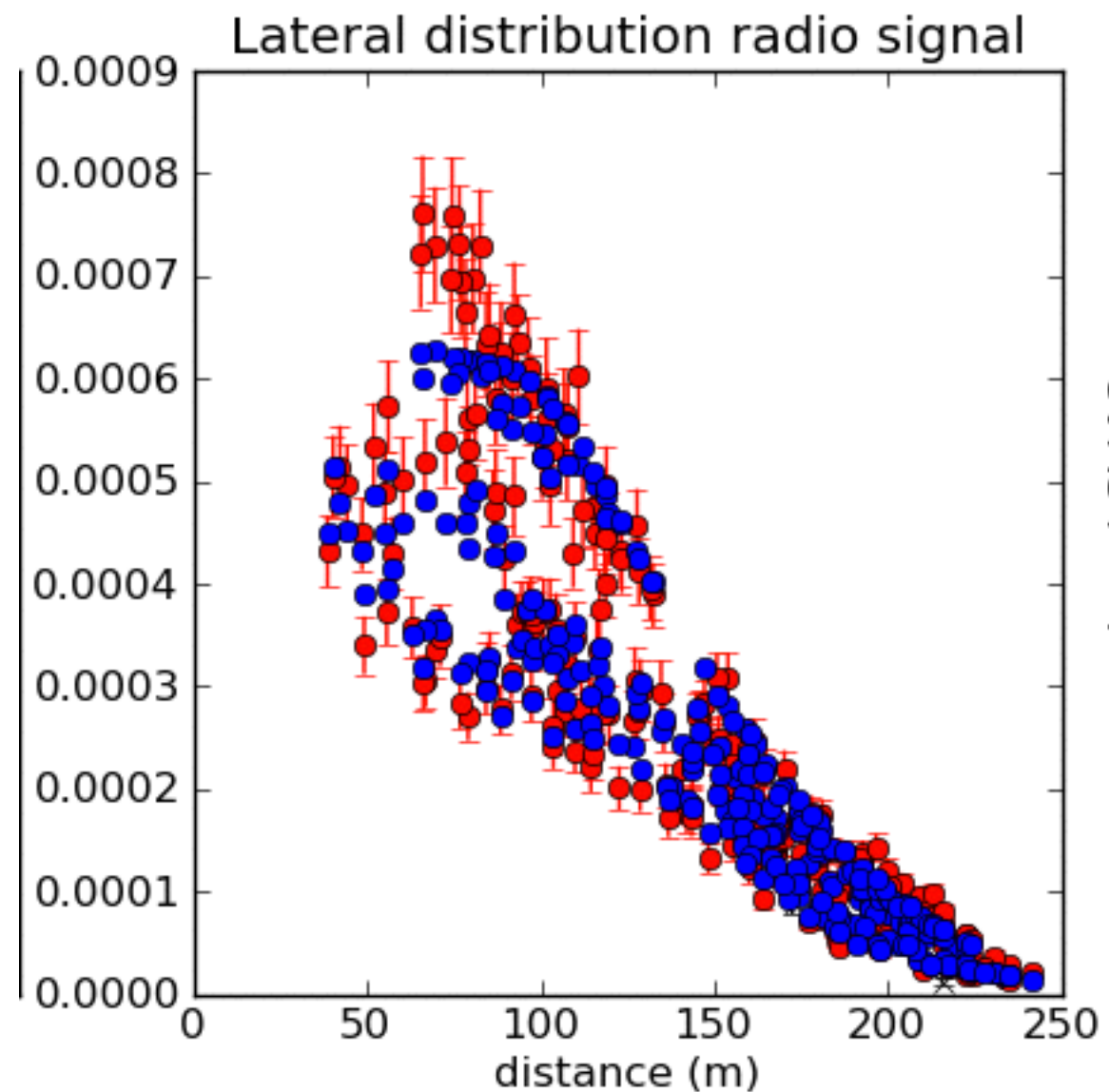
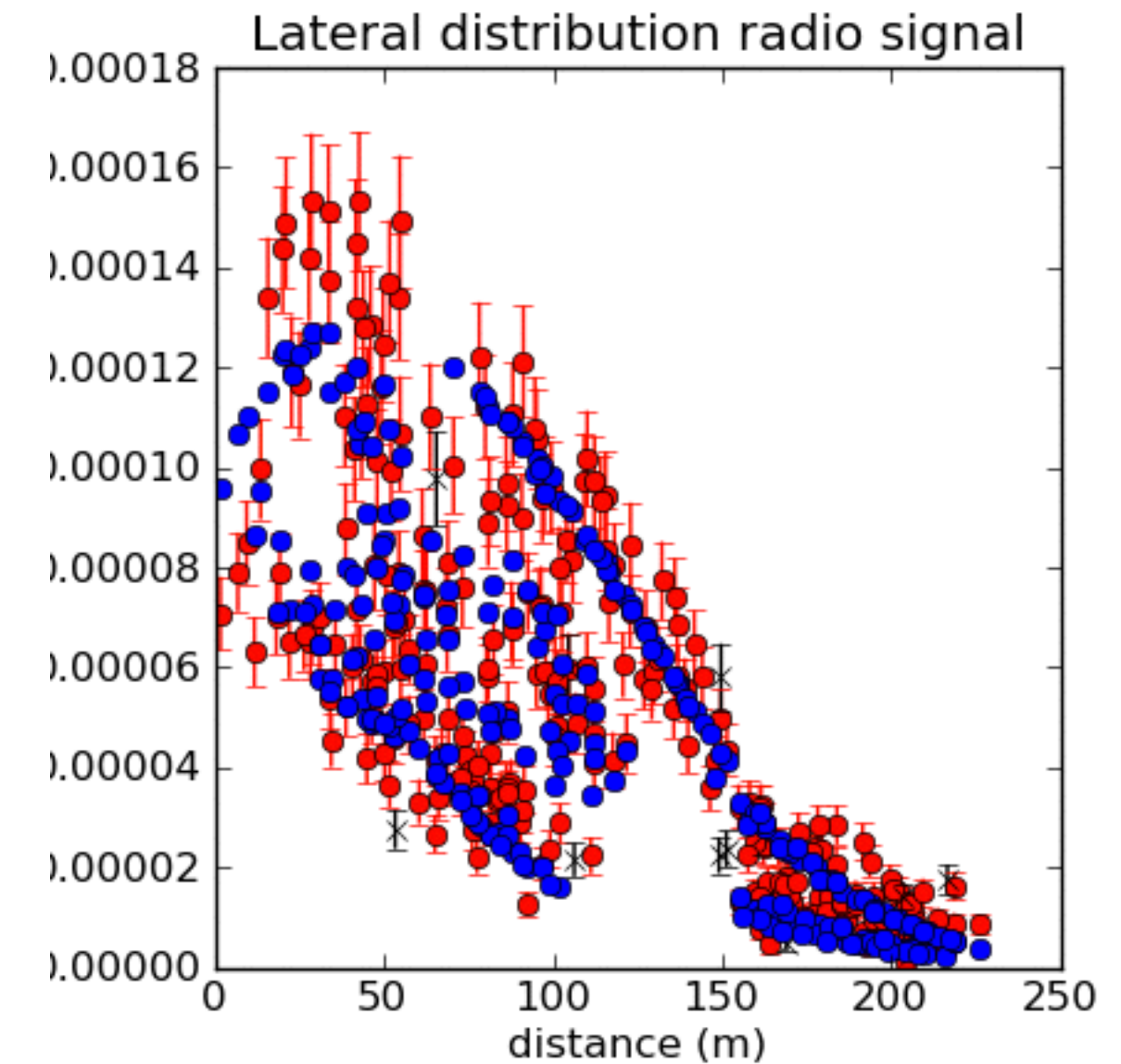
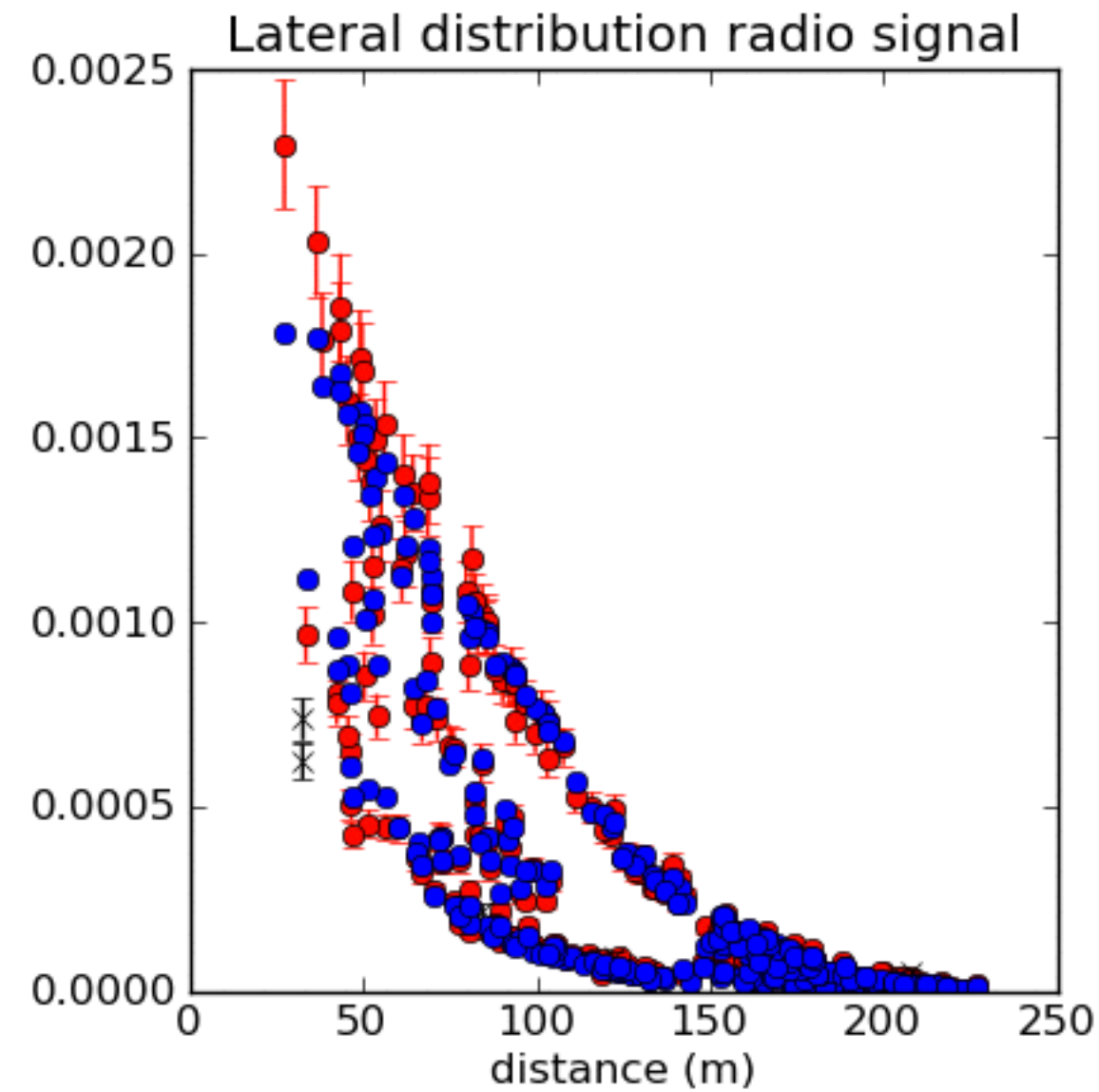
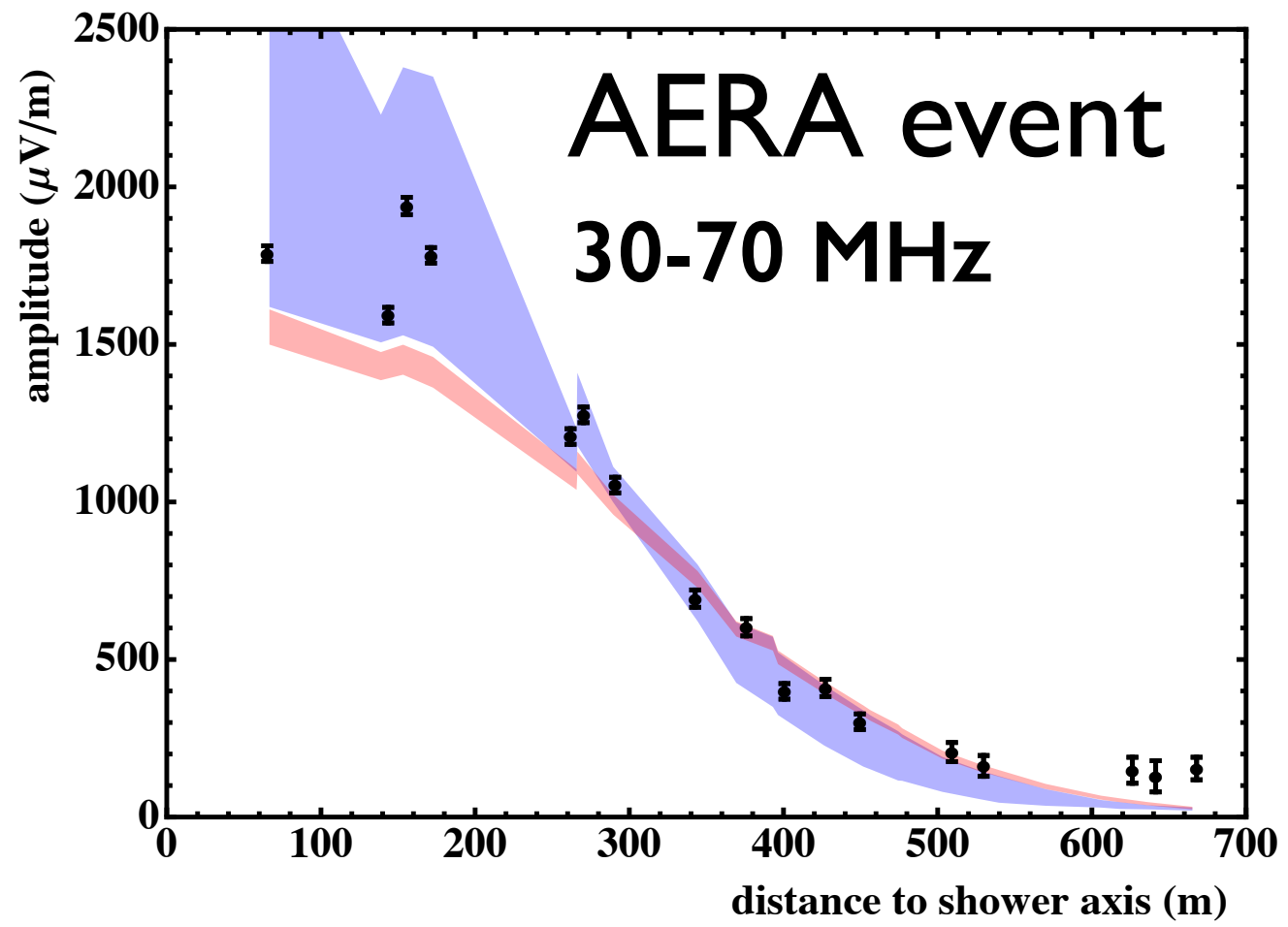
Charge excess contribution

$$+ \frac{1}{c} \frac{\partial}{\partial t} \sum_{i=1}^N \frac{q_i \vec{n}_i}{R_i (1 - \eta \vec{\beta}_i \cdot \vec{n}_i)}$$





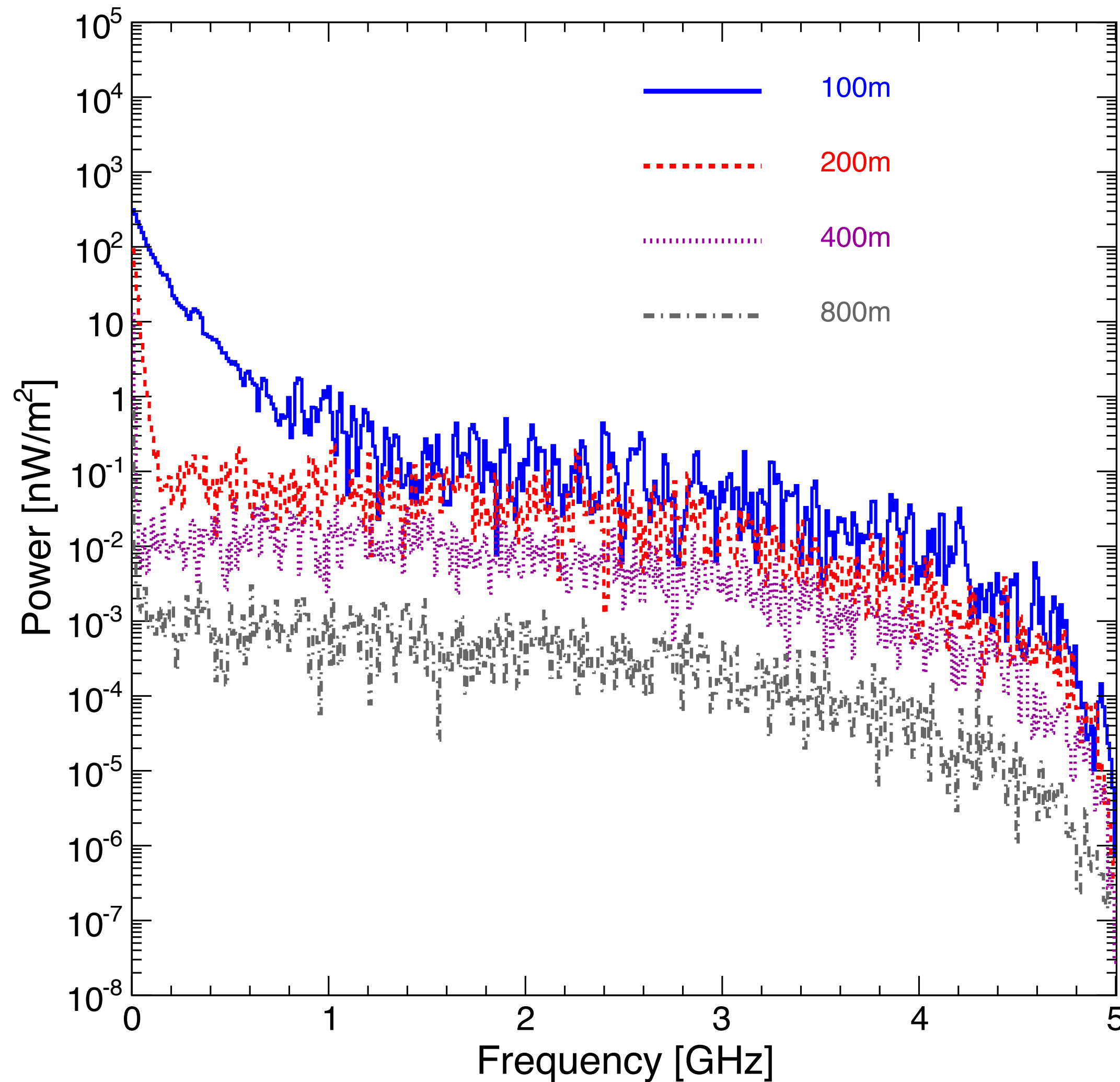
# Comparison with single events



(LOFAR plots by S. Buitink)

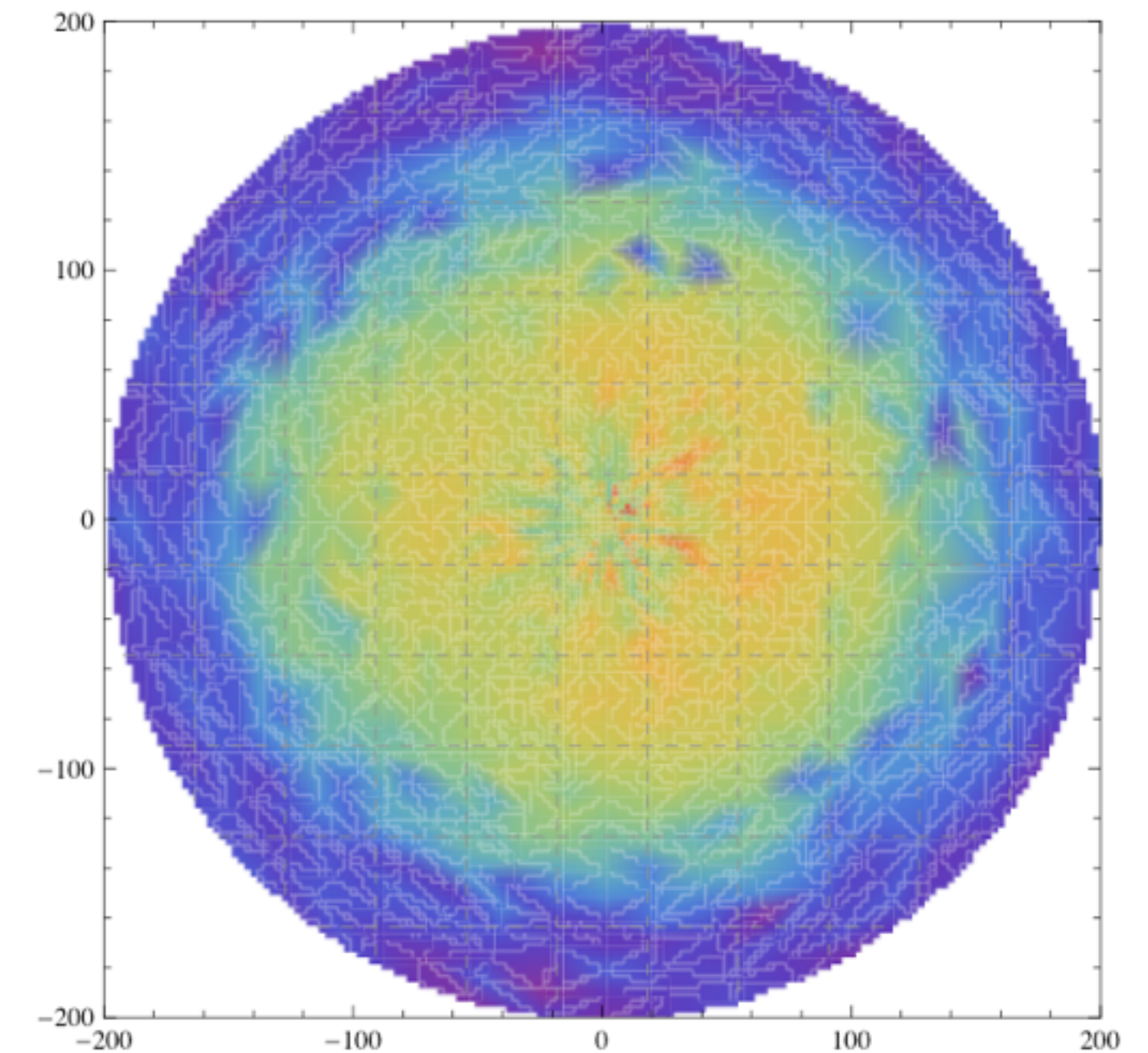
# Up to some GHz

EW: Along East axis /  $n_{\text{REAL}}$



extend the mechanisms observed in the MHz domain to the GHz domain  
take into account the effect of a realistic refractive index

Proton

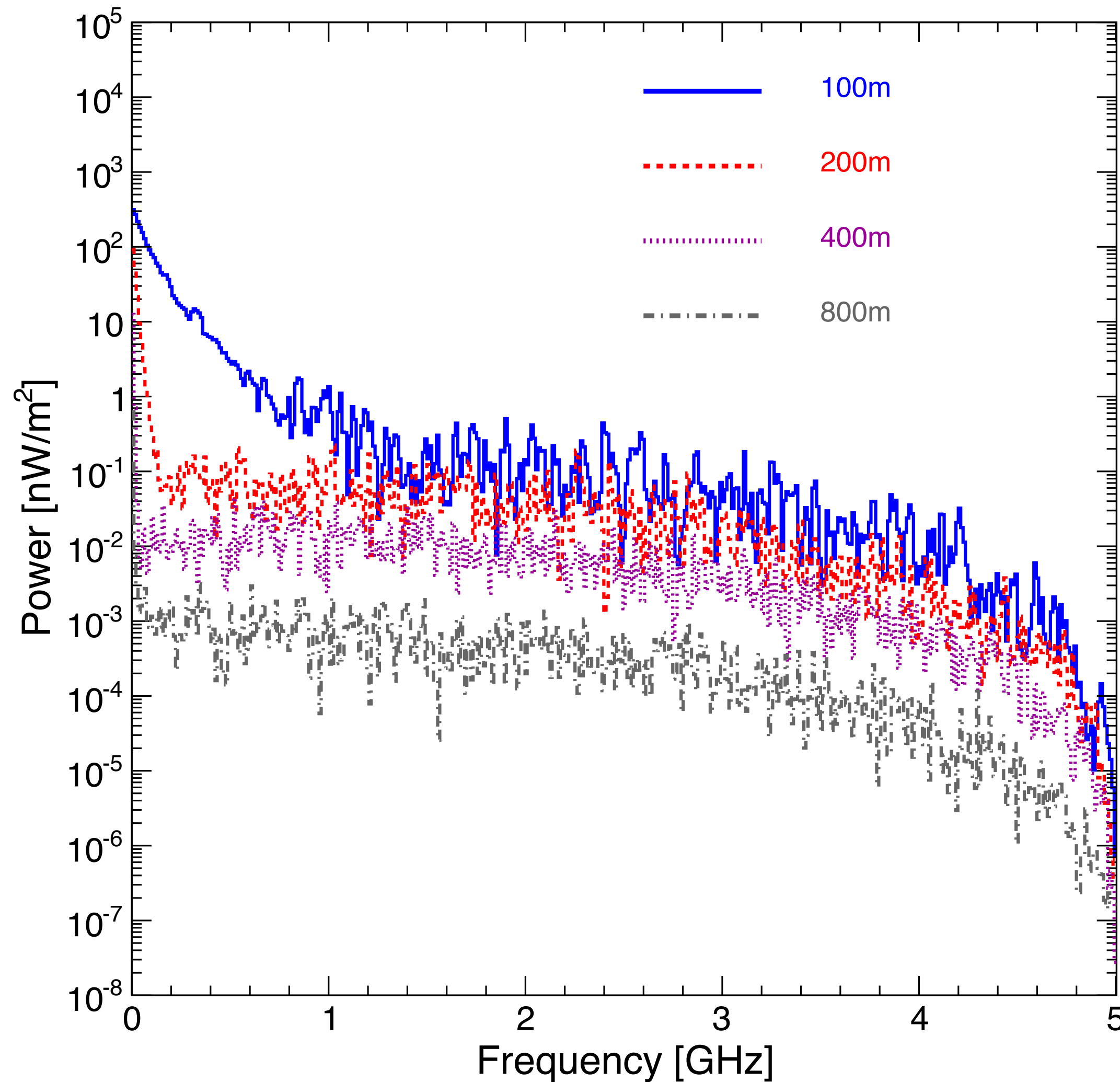


300 MHz - 1.2 GHz



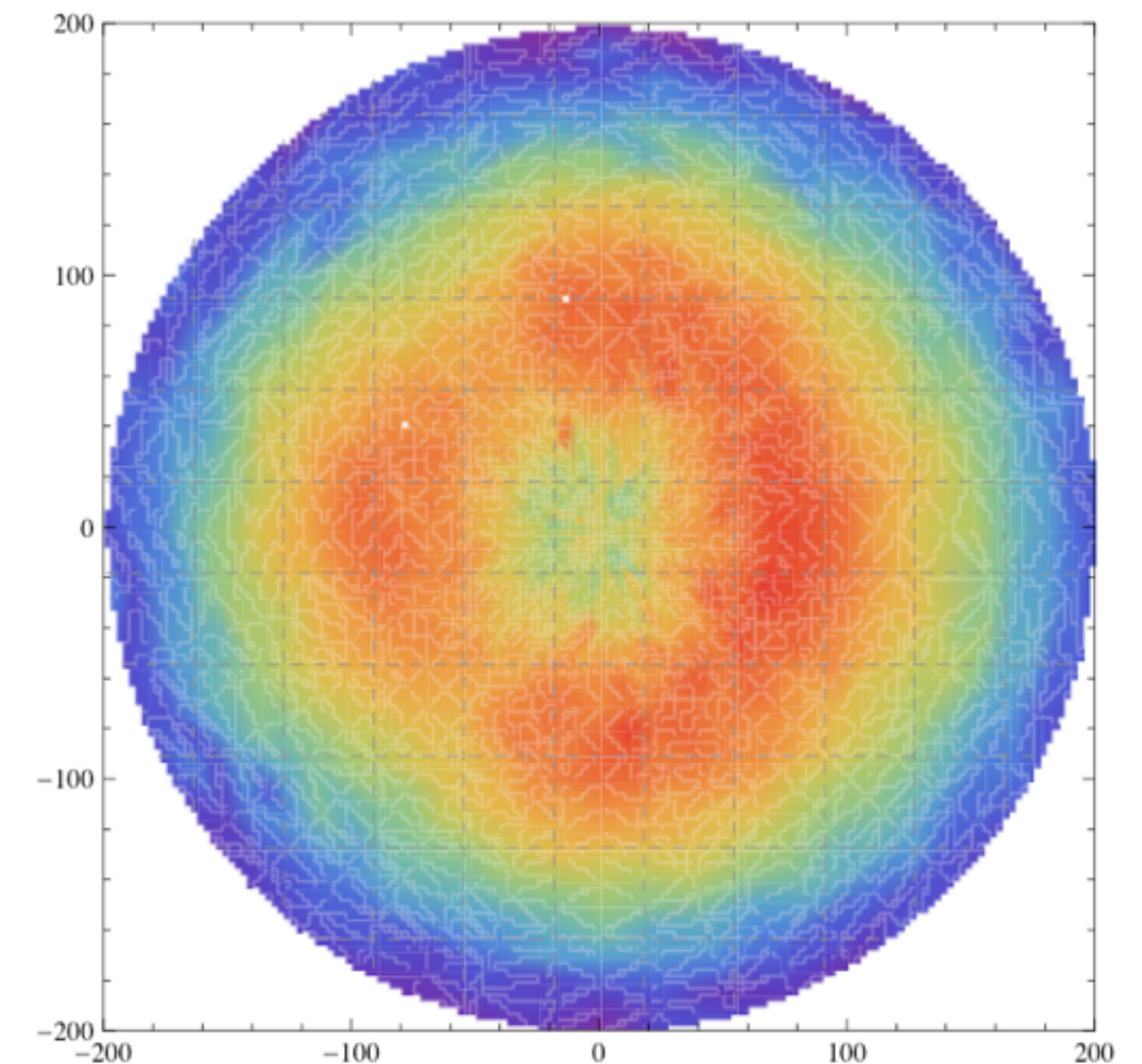
# Up to some GHz

EW: Along East axis /  $n_{\text{REAL}}$



extend the mechanisms observed in the MHz domain to the GHz domain  
take into account the effect of a realistic refractive index

Iron



**300 MHz - 1.2 GHz**

No MBR evidence in the GHz signal

# Down to some kHz

Predicted mechanisms:

contribution of the usual geomagnetic and charge excess contributions during the shower development in the air

+

the transition radiation when the shower front hits the ground

+

the coherent Bremsstrahlung of  $e^+/e^-$  when they reach the ground level  
[Revenu ICRC2013, Rio]

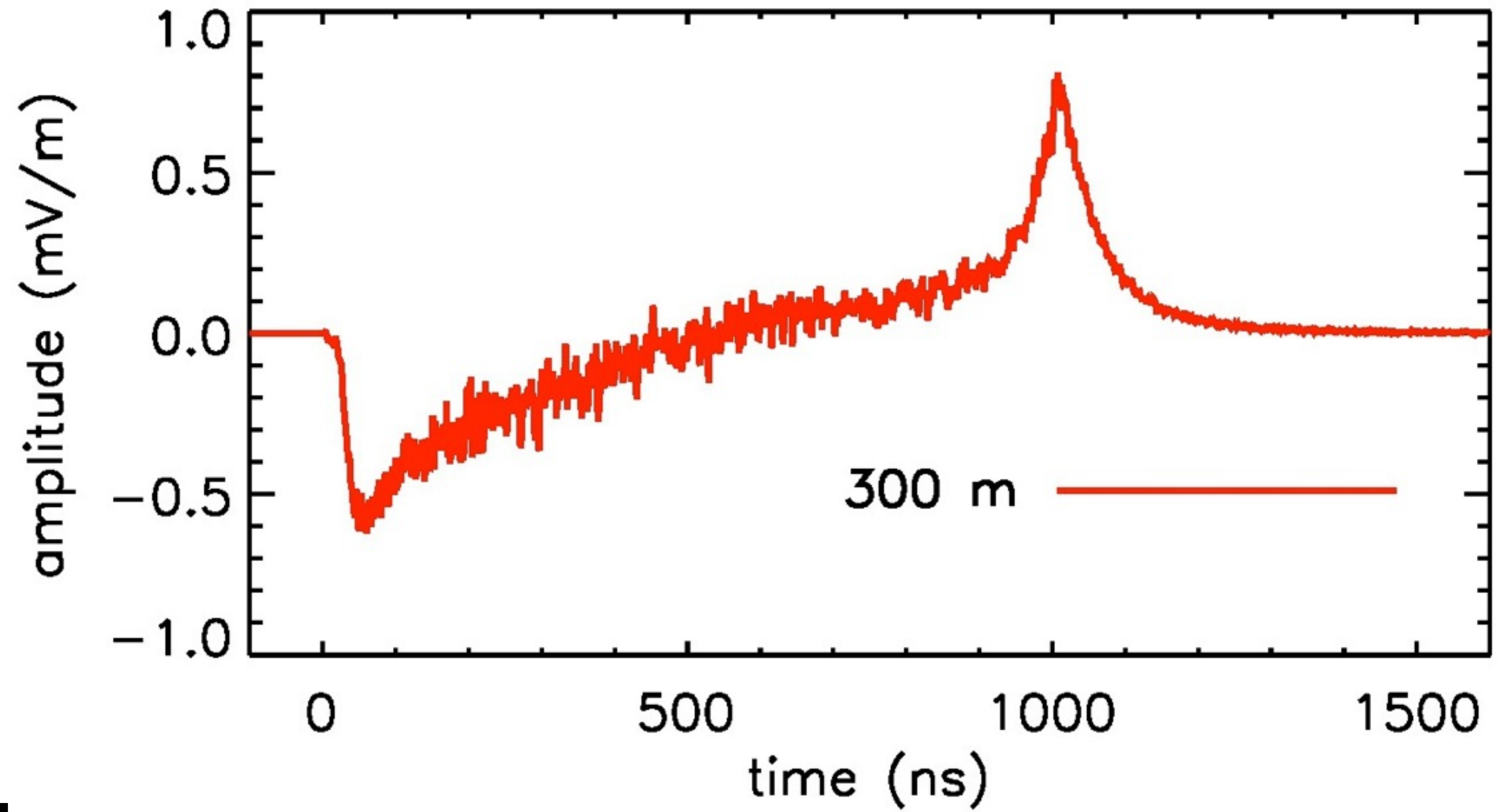
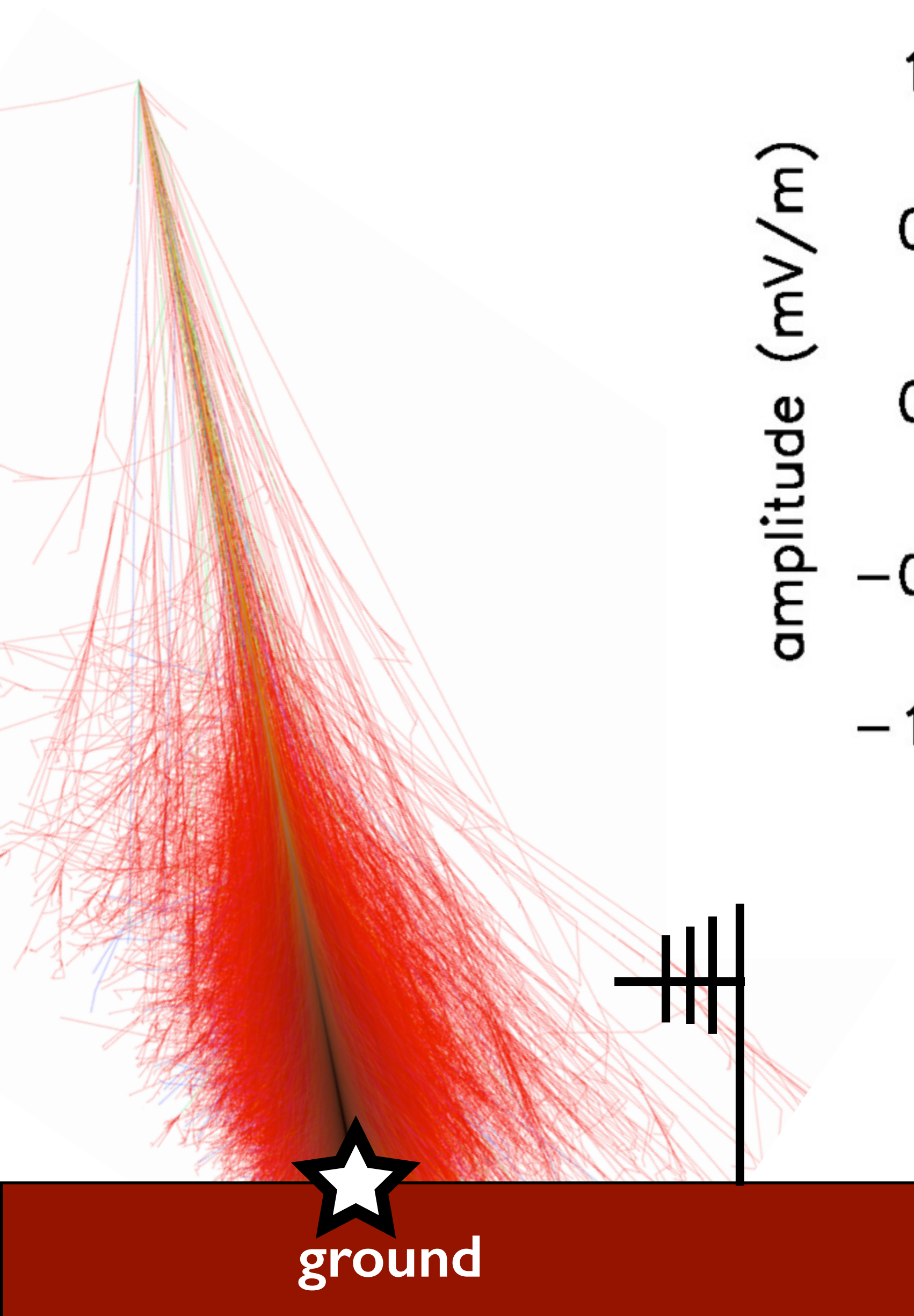
**sudden death**  
of the shower

$$\vec{E}(\vec{x}, t) = \frac{1}{4\pi\epsilon_0 c} \frac{\partial}{\partial t} \sum_{i=1}^N q_i \left( \frac{\vec{\beta}_i - (\vec{n}_i \cdot \vec{\beta}_i) \vec{n}_i}{R_i (1 - \eta \vec{\beta}_i \cdot \vec{n}_i)} \right)_{\text{ret}} \quad (\text{Coulomb gauge})$$

New contribution below 20 MHz, **vertical** polarization,  
**monopolar** pulse with amplitude decreasing with  $1/d_{\text{core}}$   
(as already observed in the past by AGASA, Gauhati group, EAS-radio...)

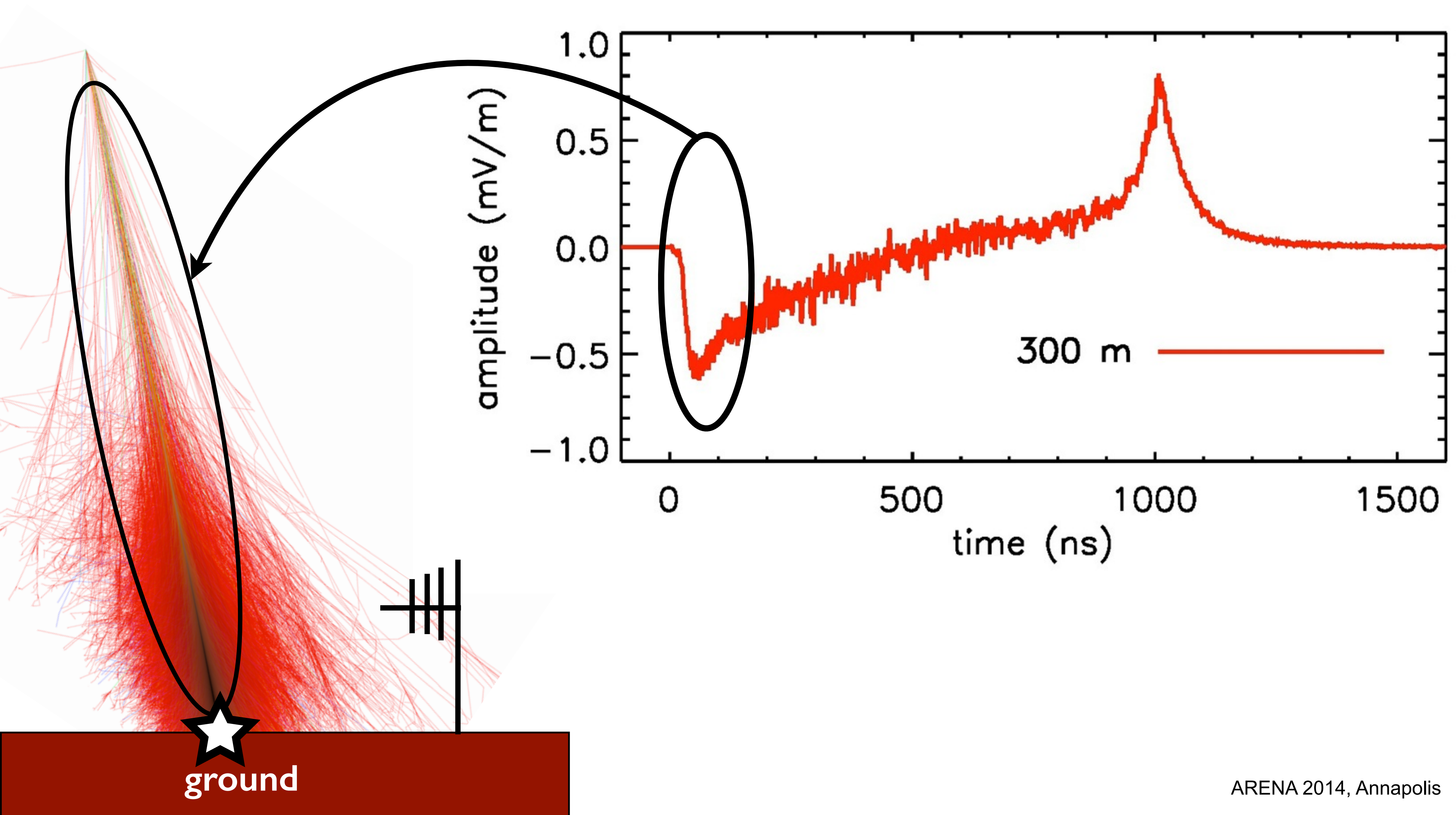


# Down to some kHz



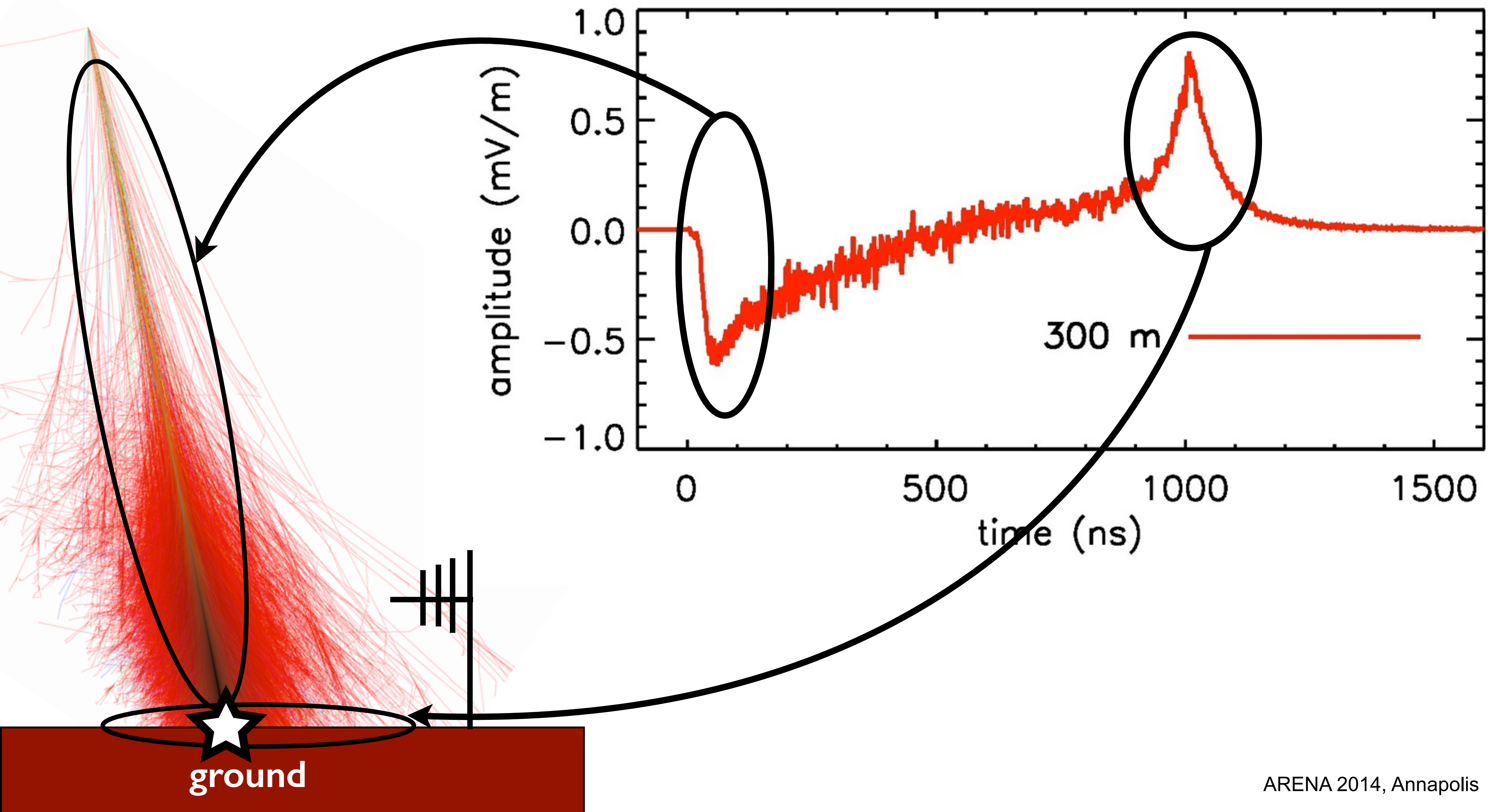


# Down to some kHz





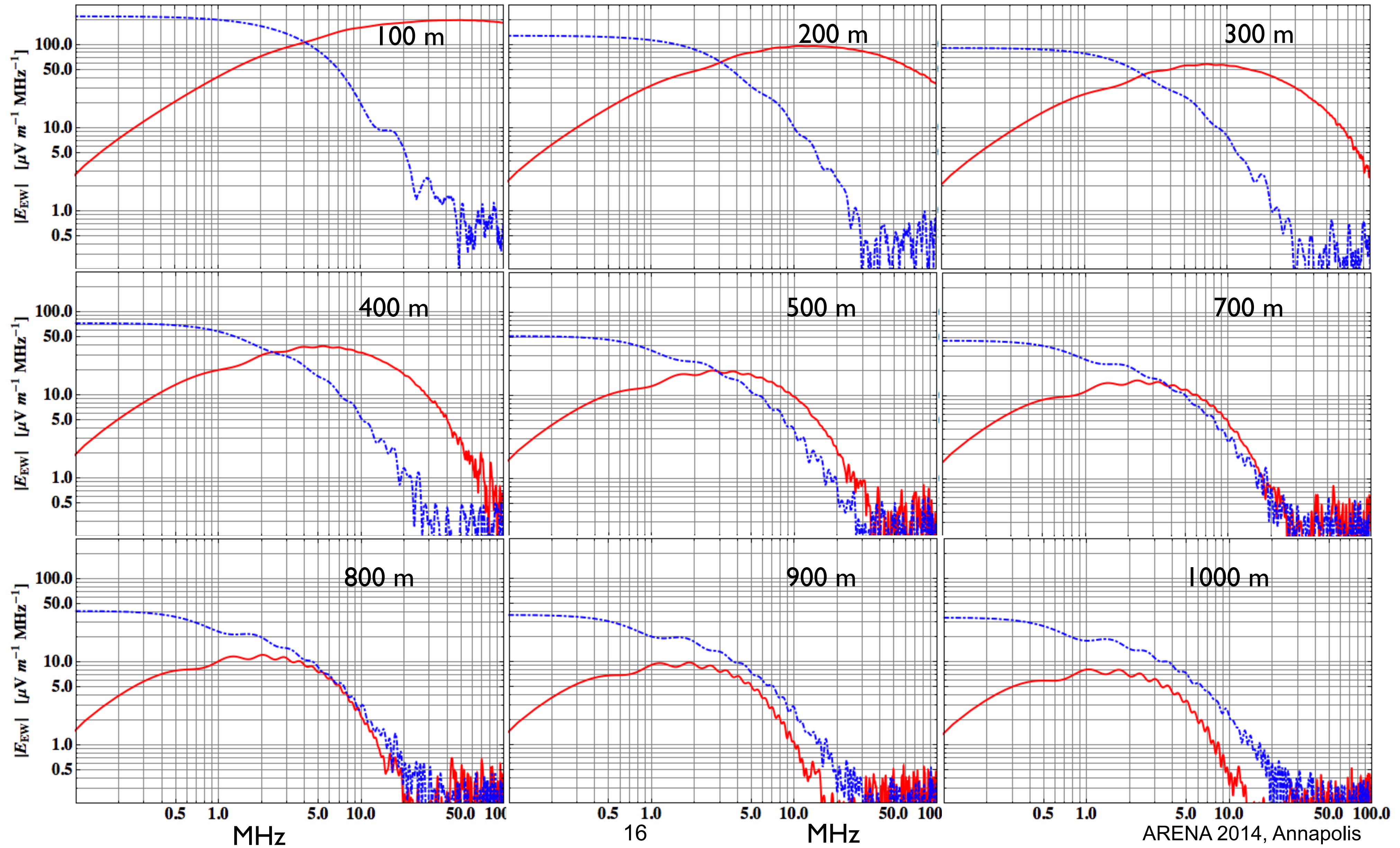
# Down to some kHz





ground contribution  
development in the air

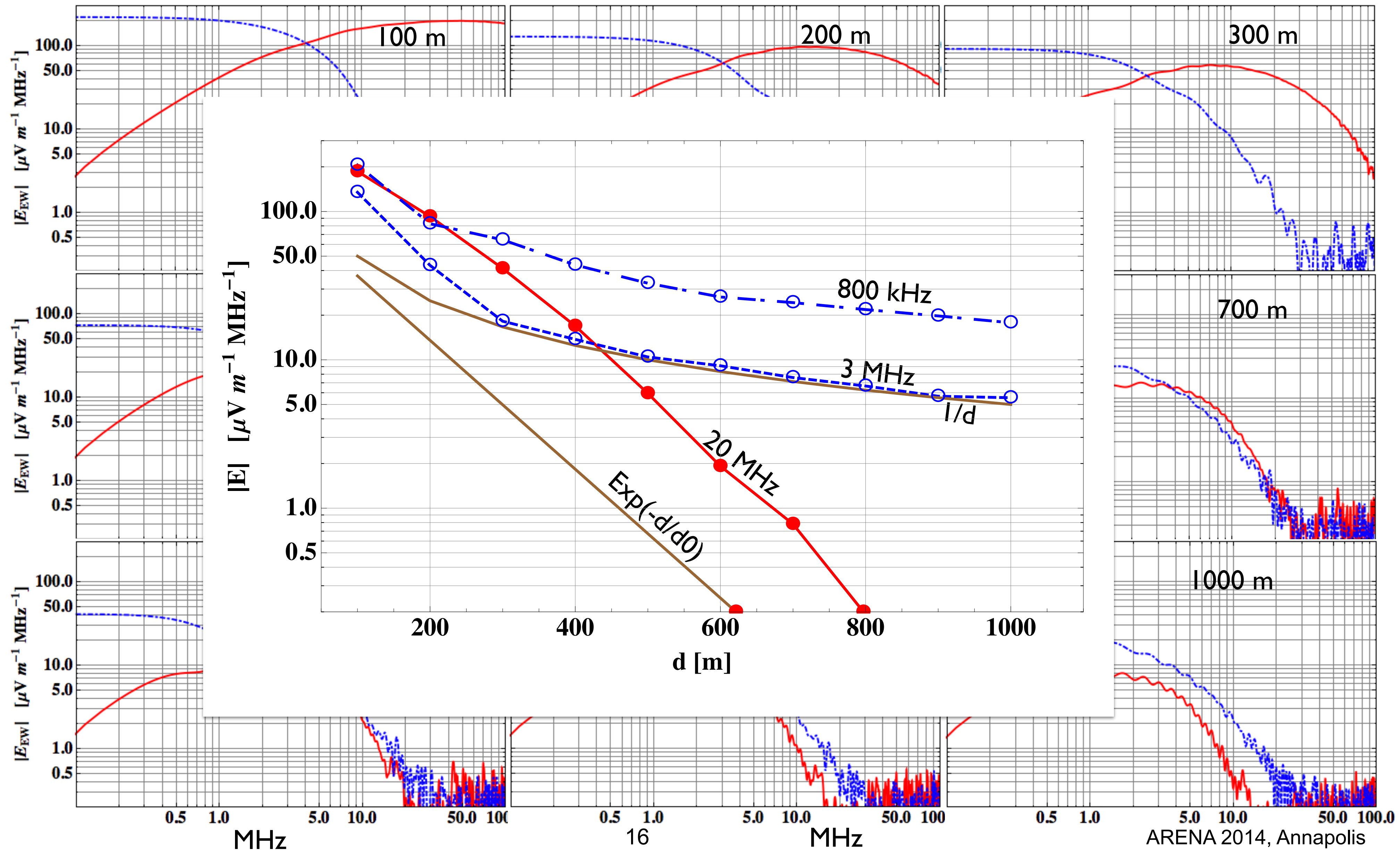
# Down to some kHz





ground contribution  
development in the air

# Down to some kHz



# Conclusion

- SELFAS is a simple code, easy to use and fast: good for extensive use event by event
- it describes well the data (RAuger, CODALEMA, AERA, LOFAR...) in the range 20-200 MHz
- CONEX is used to generate the longitudinal profile
- the radio emission is now well understood
- at lower frequencies, a new phenomenon appears: the electric field emission by the shower sudden death when reaching the ground  
EXTASIS is a dedicated experiment in Nançay, inside CODALEMA, under progress