

SEFEAS2

**Simulation of Electric Field emitted by Air
Shower**

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SELFAS2

• Concept

• Formalism,
electric field

• Field at
shower scale

• 10^{17} eV
Vertical event

• SELFAS2 at
CODALEMA

• SELFAS2 at
RAuger1

• Realistic air
refractive index

• Conclusion

➔ Dedicated to radio emission in the MHz range

➔ Create an autonomous code which doesn't launch any full shower simulation (CORSIKA, AIRES)

➔ Based on air shower universality

➔ Using relevant universal distributions :

-GIL Longitudinal profile Greisen, Iljina, Linsley in Proc. of 27th ICRC

-Energy distribution

-Vertical and horizontal momentum direction

-lateral distribution

-Delay time (shower front thickness)

Lafebre et al
AP, 31(3):243–254 2009

➔ Generate only e^+ and e^- of the shower front (3D)

➔ Track each e^+/e^- along their trajectory to compute and sum up all individual field contribution at any observation point

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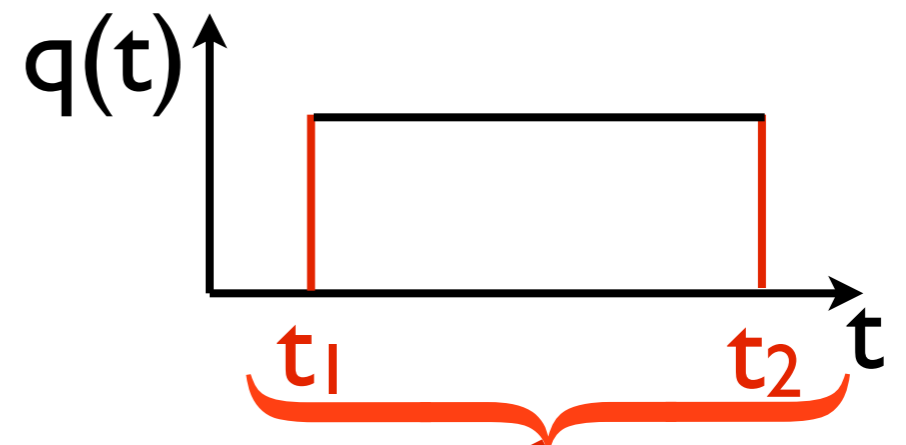
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Individual charge with a finite life time

t_1 = start point time

t_2 = end point time



Charge density $\rho(\mathbf{x}', t')$ = $q[\theta(t' - t_1) - \theta(t' - t_2)]\delta^3(\mathbf{x}' - \mathbf{x}_0(t'))$

Current density $\mathbf{J}(\mathbf{x}', t')$ = $\rho(\mathbf{x}', t')\mathbf{v}(t')$

With Maxwell equations : (Lorenz gauge)

$$\mathbf{E}(\mathbf{x}, t) = \frac{1}{4\pi\epsilon_0} \int d^3x' dt' \frac{1}{R} \left[-\nabla' \rho - \frac{1}{c^2} \frac{\partial \mathbf{J}}{\partial t'} \right]_{\text{ret}} \delta \left\{ t' - \left(t - \frac{|\mathbf{x} - \mathbf{x}'|}{c} \right) \right\}$$

Performing time and spatial integrations :

$$\mathbf{E}(\mathbf{x}, t) = \frac{1}{4\pi\epsilon_0} \left\{ \left[\frac{\mathbf{n}q(t_{\text{ret}})}{R^2(1 - \boldsymbol{\beta} \cdot \mathbf{n})} \right]_{\text{ret}} + \frac{1}{c} \frac{\partial}{\partial t} \left[\frac{\mathbf{n}q(t_{\text{ret}})}{R(1 - \boldsymbol{\beta} \cdot \mathbf{n})} \right]_{\text{ret}} - \frac{1}{c^2} \frac{\partial}{\partial t} \left[\frac{\mathbf{v}q(t_{\text{ret}})}{R(1 - \boldsymbol{\beta} \cdot \mathbf{n})} \right]_{\text{ret}} \right\}$$

In SELFAS2 previous version :

Refractive index fixed to unity \Rightarrow No Cerenkov effects

At shower scale : summing up all contributions

$$E_{tot}(\mathbf{x}, t) = \frac{1}{4\pi\epsilon_0} \left\{ \sum_{i=1} \left[\frac{n_i q_i(t_{ret})}{R_i^2 (1 - \beta_i \cdot \mathbf{n}_i)} \right]_{ret} + \frac{1}{c} \frac{\partial}{\partial t} \sum_{i=1} \left[\frac{n_i q_i(t_{ret})}{R_i (1 - \beta_i \cdot \mathbf{n}_i)} \right]_{ret} - \frac{1}{c^2} \frac{\partial}{\partial t} \sum_{i=1} \left[\frac{\mathbf{v}_i q_i(t_{ret})}{R_i (1 - \beta_i \cdot \mathbf{n}_i)} \right]_{ret} \right\}$$

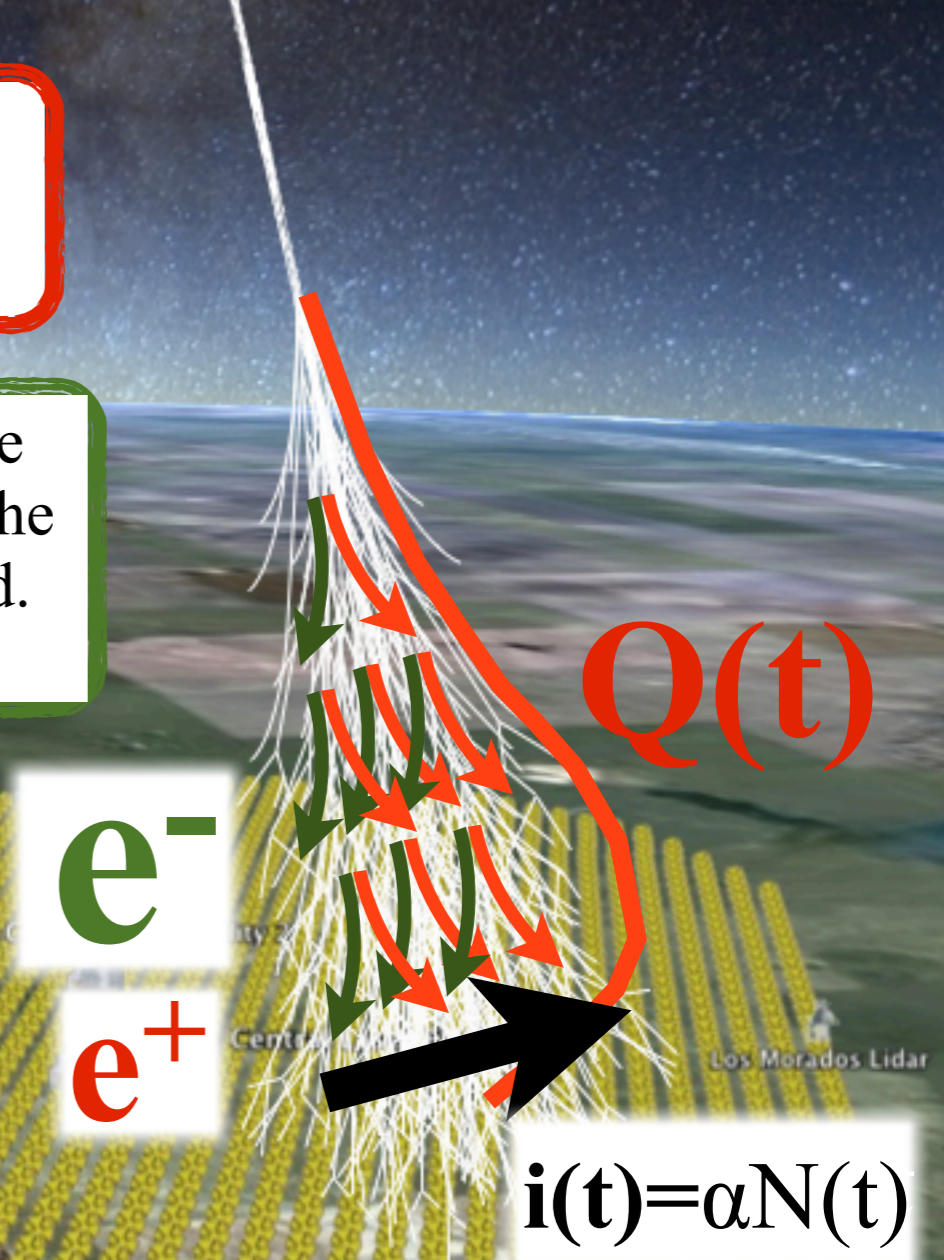
global Coulombian Summation of all individual static contributions.

≈ two orders of magnitude smaller

Charge excess variation Due to the e⁻ in excess
Q(t) = α N(t)

Transverse current variation Systematic opposite drift of e⁻ and e⁺ in the earth magnetic field.

Dominant, except for showers parallel to the geomag. field



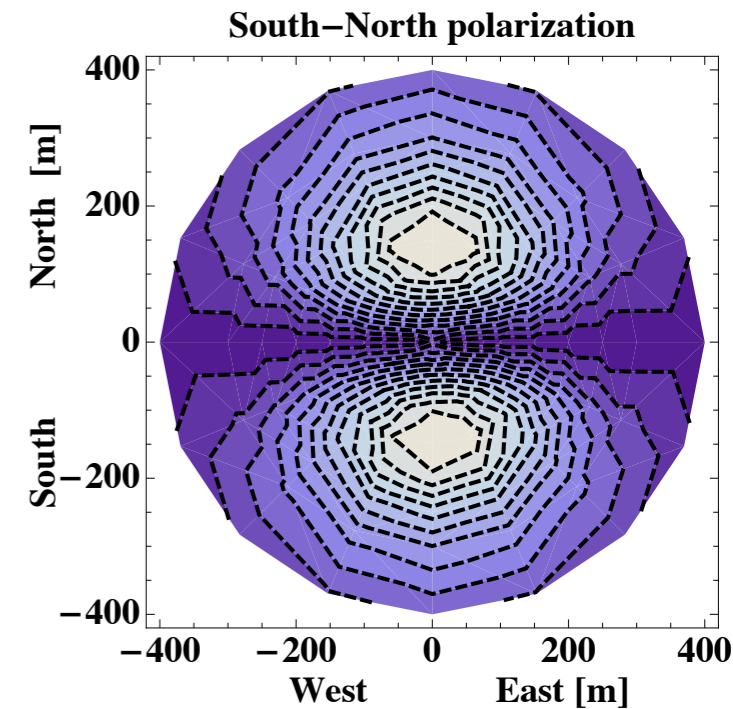
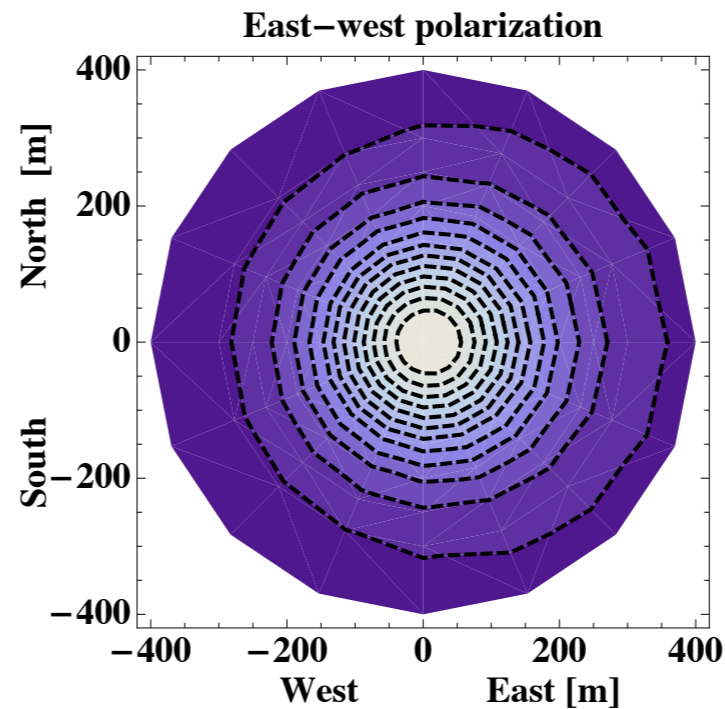
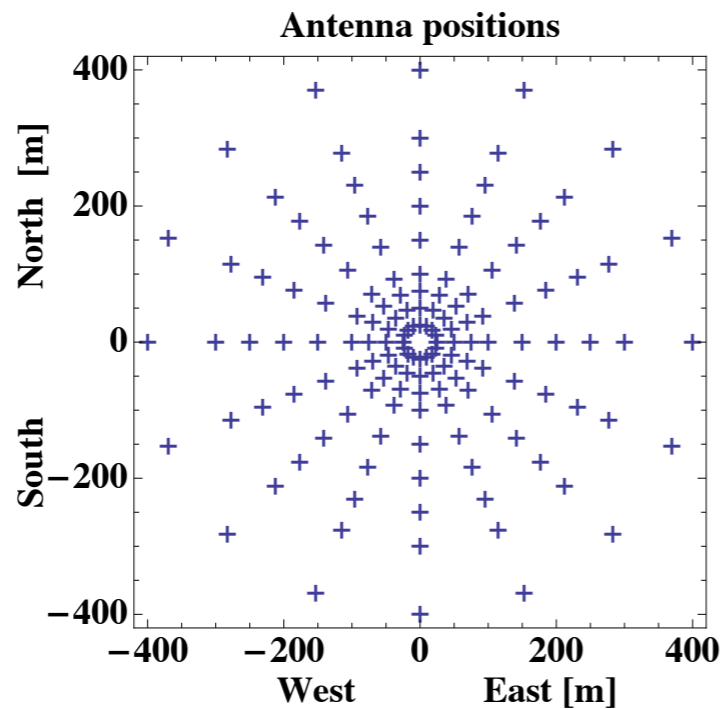
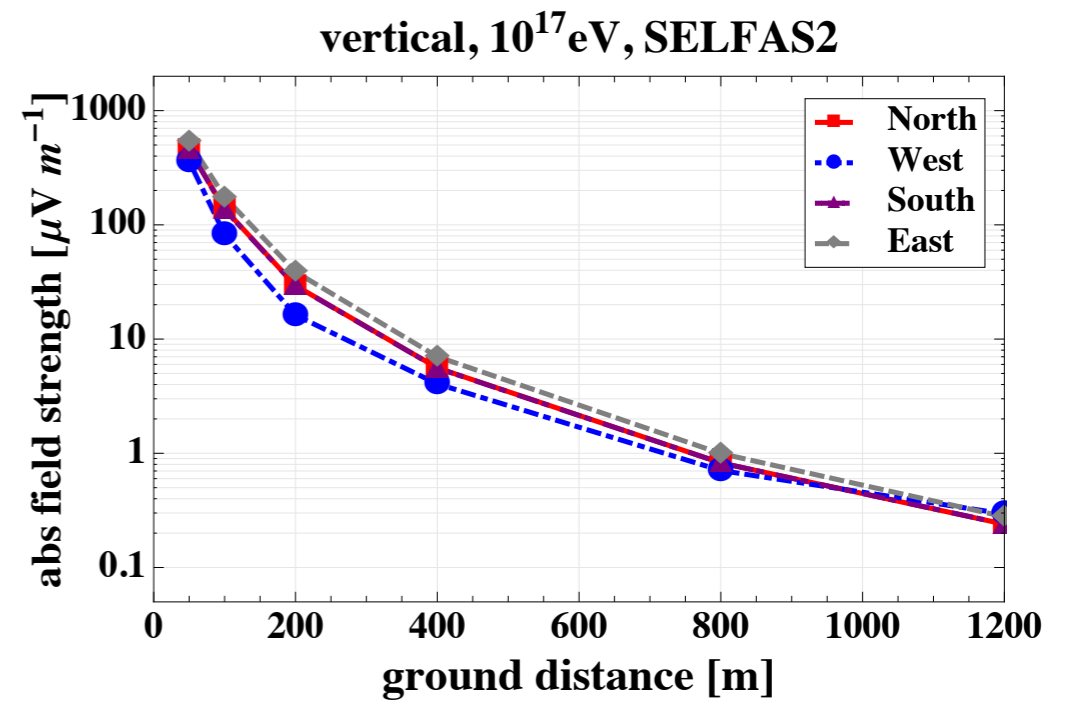
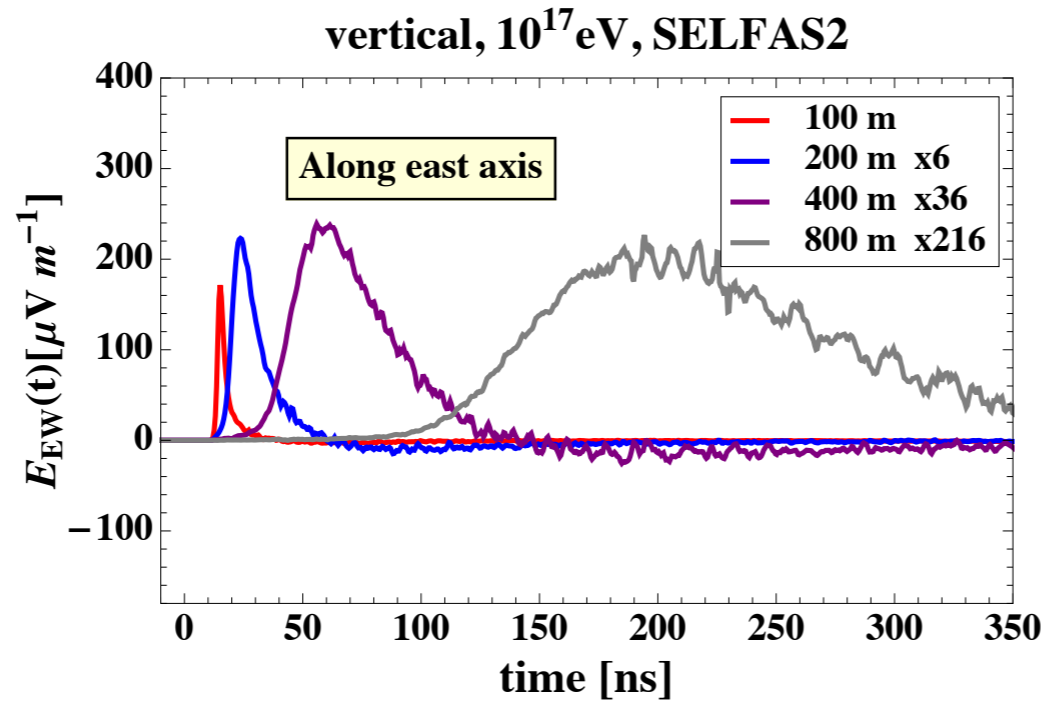
- Formalism, electric field
- **Field at shower scale**
- 10¹⁷ eV
- Vertical event
- SELFAS2 at CODALEMA
- SELFAS2 at RAuger1
- Realistic air refractive index
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Example of a 10^{17} eV proton at Auger

SELFAS2 at
Astroparticle Physics
DOI : 10.1016/j.astropartphys.2012.03.007



**East-west asymmetry
due to the charge-excess contribution**

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Comparison with data

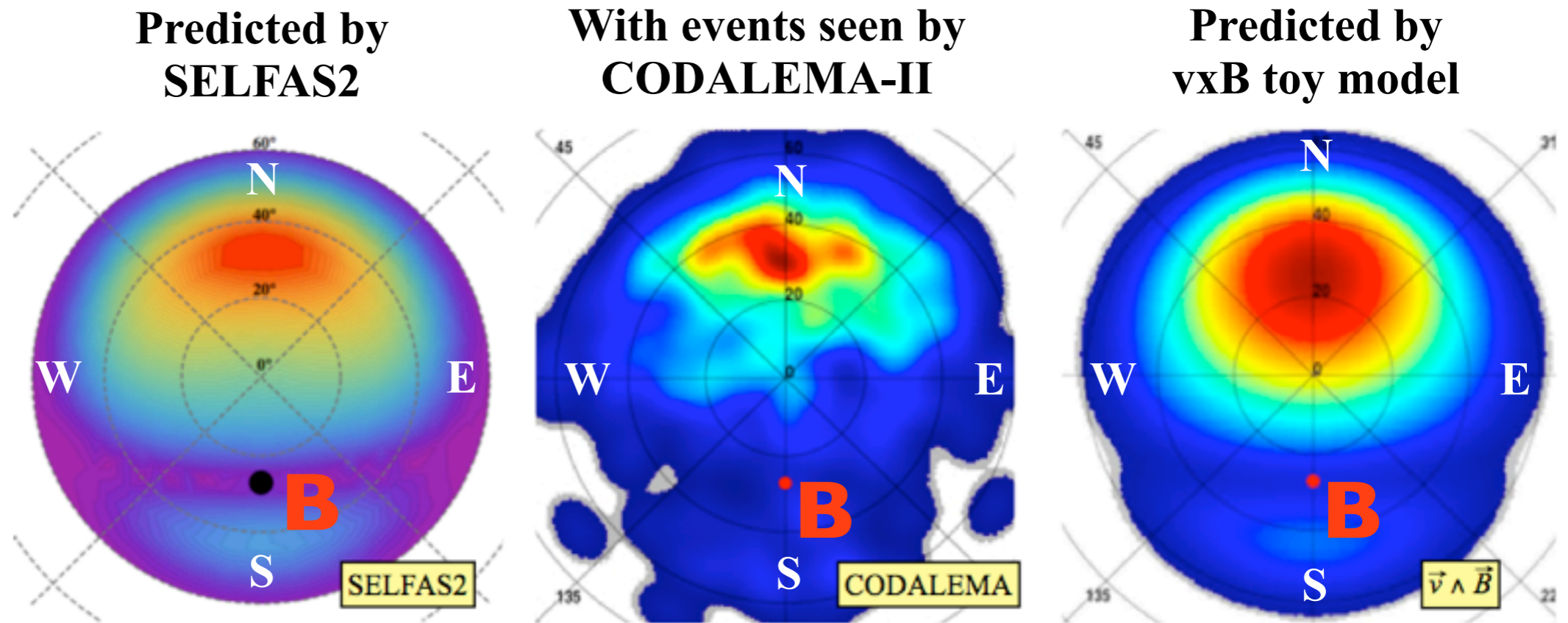
SELFAS2
(with air refractive index = 1)

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First SELFAS2 cross check with data : The arrival direction dependence

Density skymap of detected events in EW polarization for CODALEMA site



From CODALEMA 2009
A-P. 31, 3 (2009) 192-200.

More than 1 thousand events simulated around 10^{17} eV with SELFAS2, for various arrival directions

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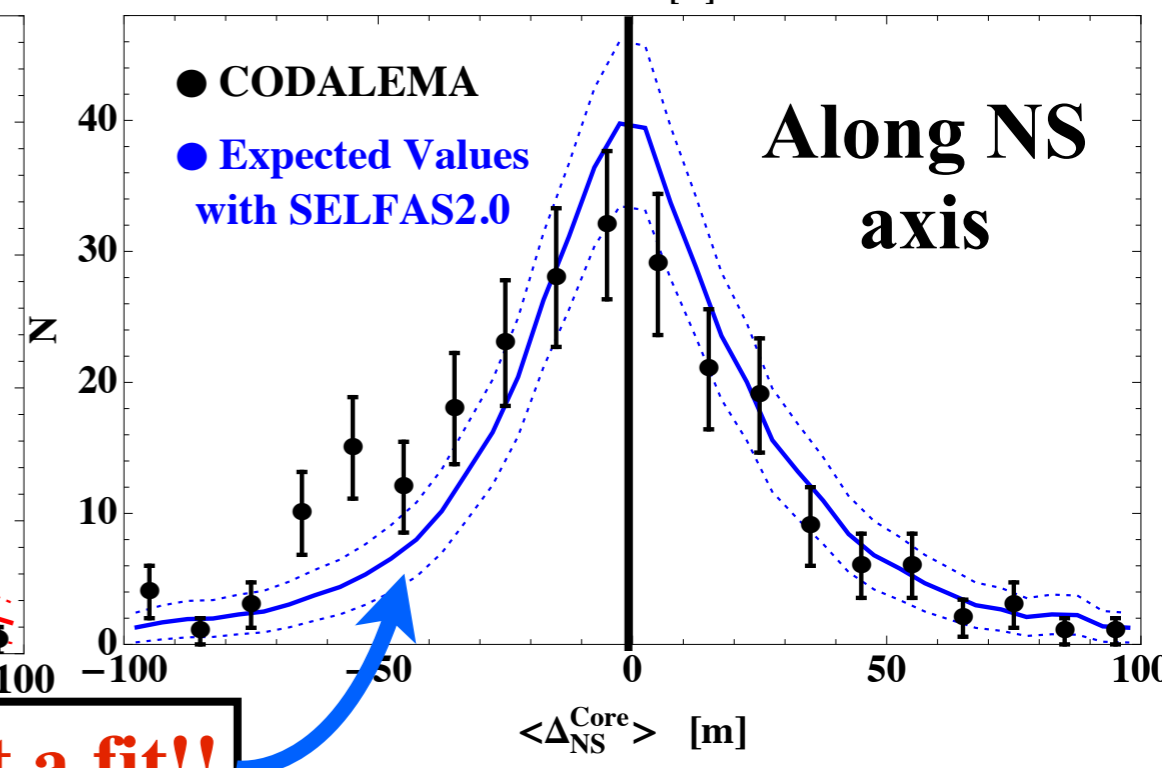
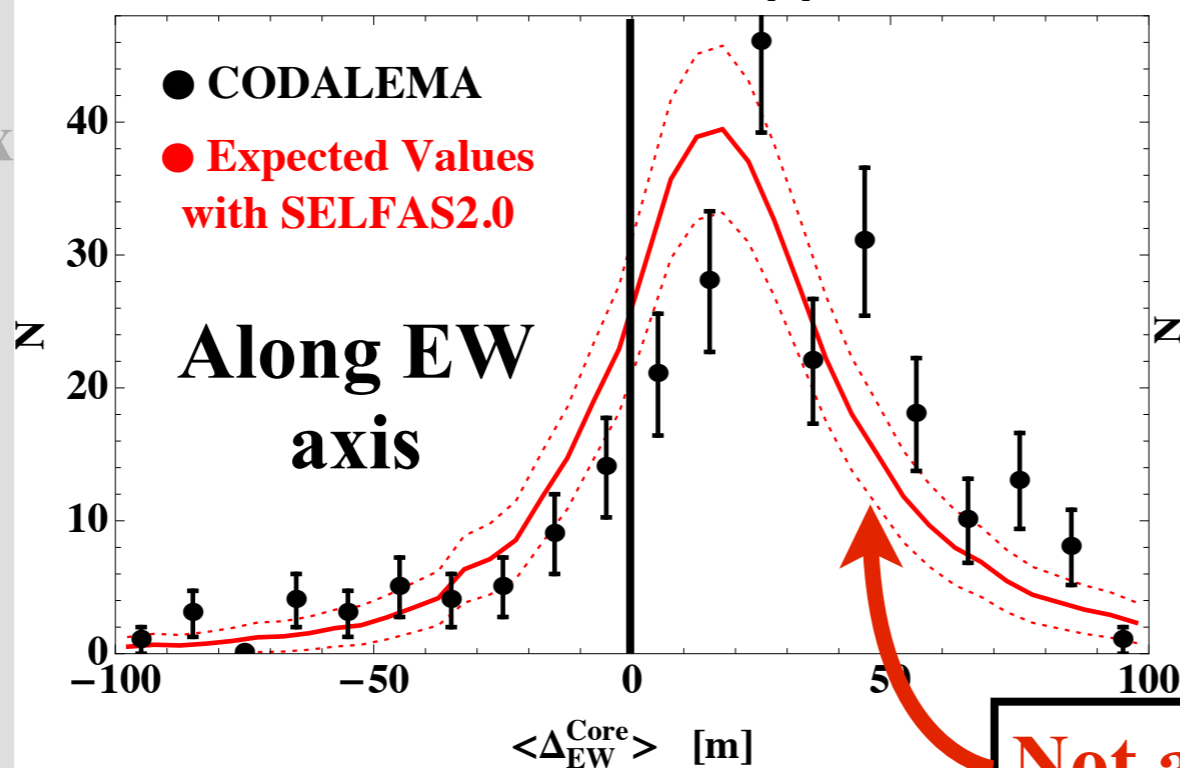
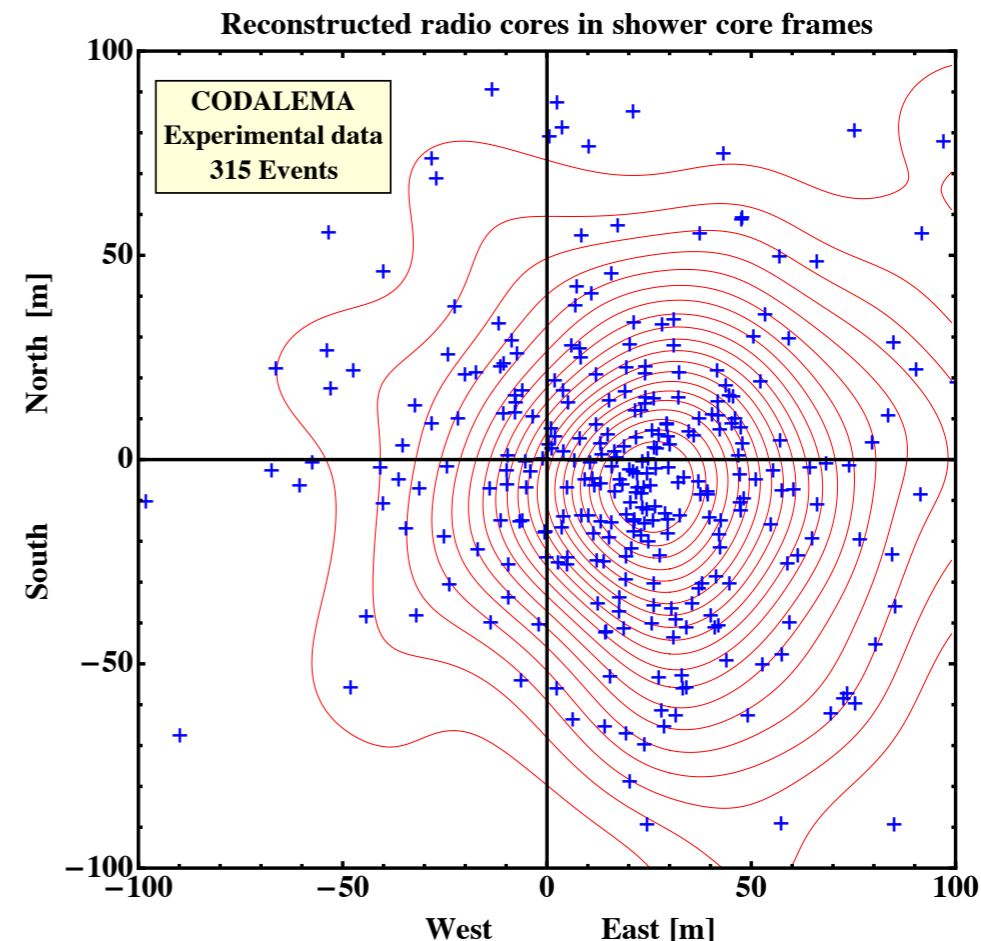
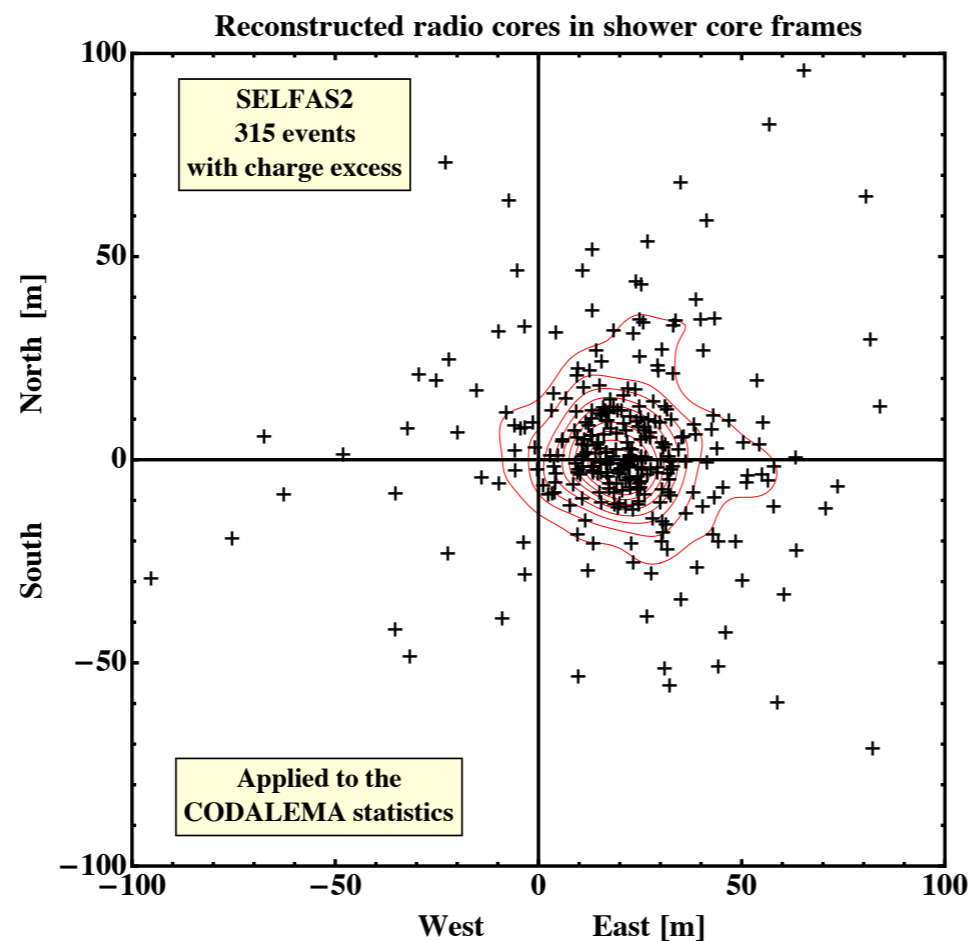
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Second SELFAS2 cross check with data : Radio core shift as charge excess signature



Not a fit!!

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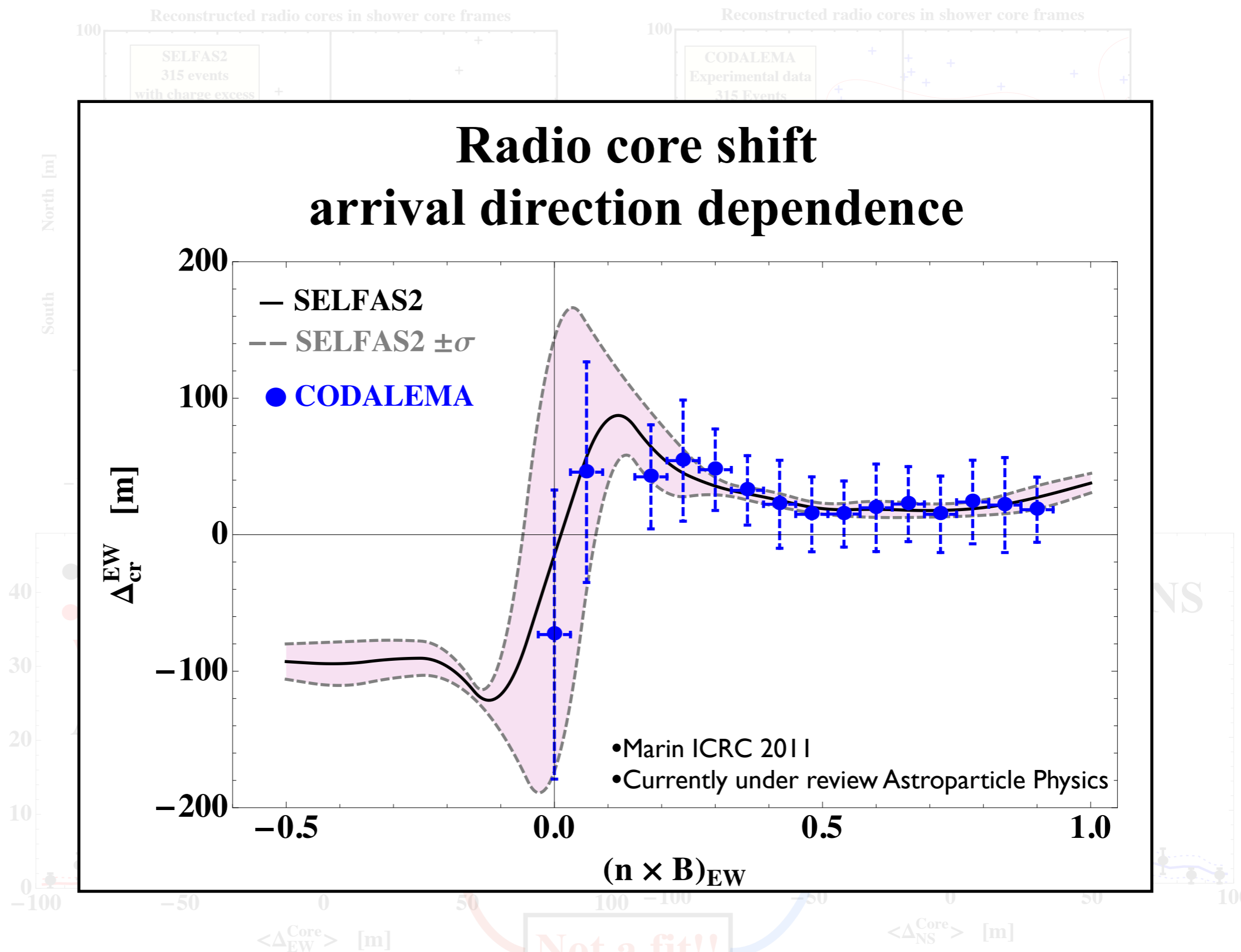
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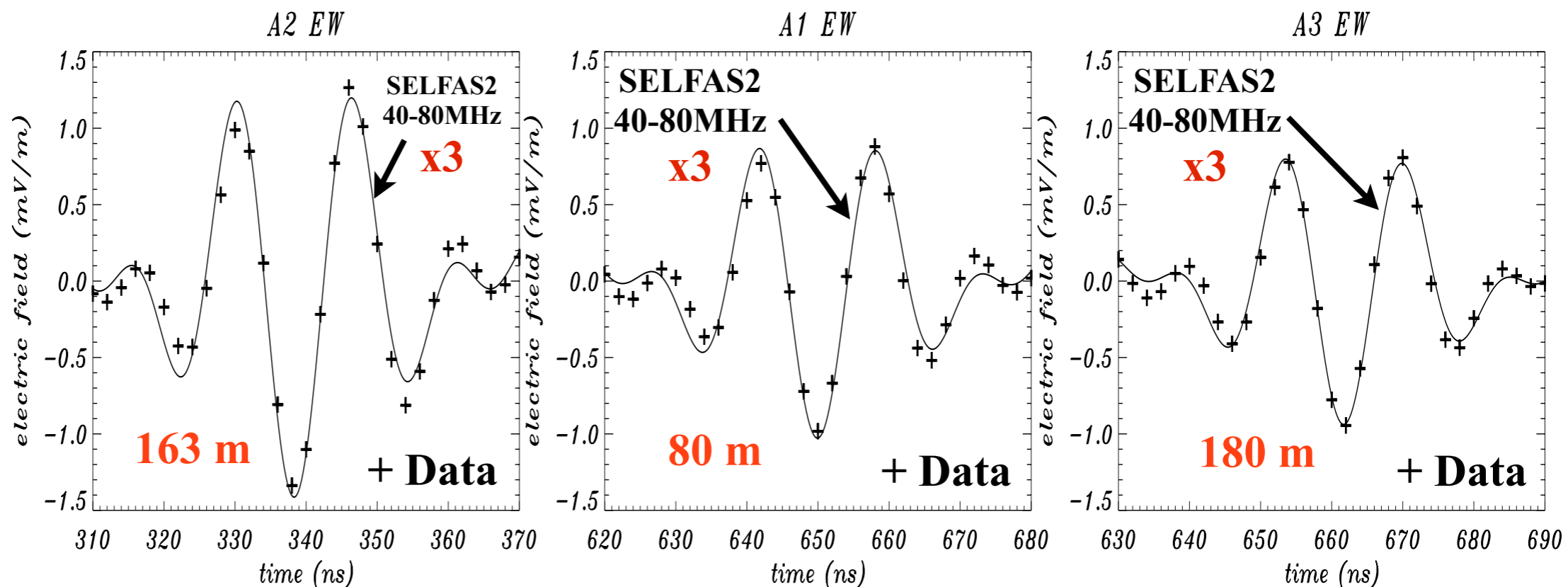
- **SELFAS2 at RAuger1**

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Third SELFAS2 cross check with data : Direct comparison with a three-fold RAuger1 event **deconvoluted from antenna response**

Filtered-band 40-80 MHz



Scaling factor of 3??

➡ Dependence to first interaction length

➡ Number of particles predicted by simulation underestimated

➡ Air refractive index not included in SELFAS2...

(but can't explain a factor of 3 in 40-80MHz region as we will see)

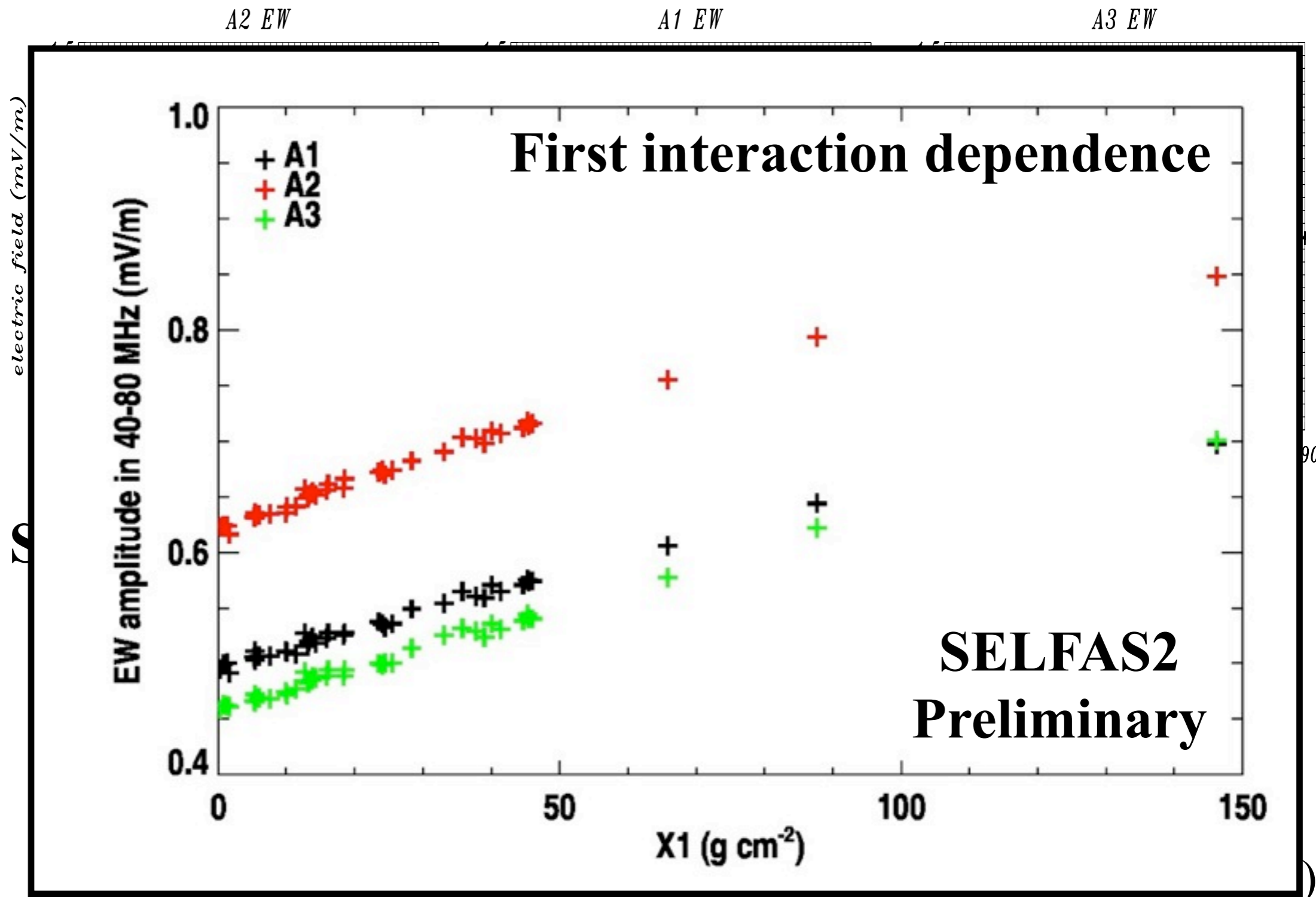
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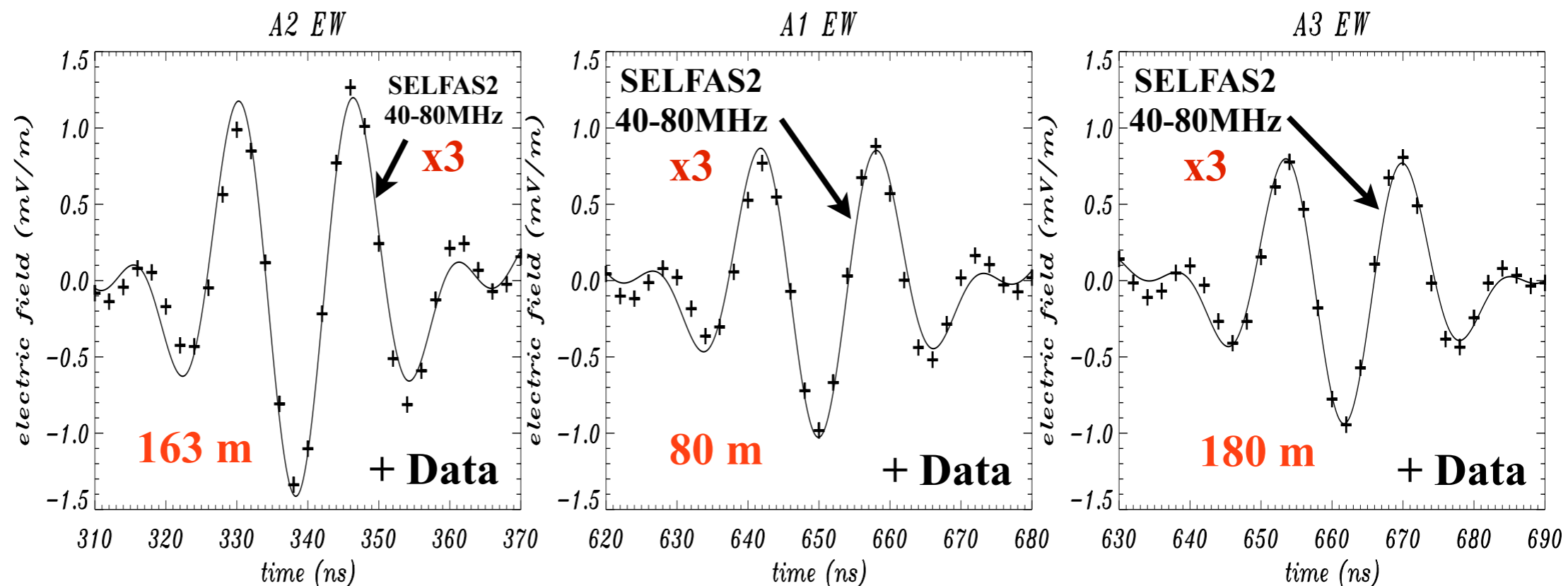
- **SELFAS2 at RAuger1**

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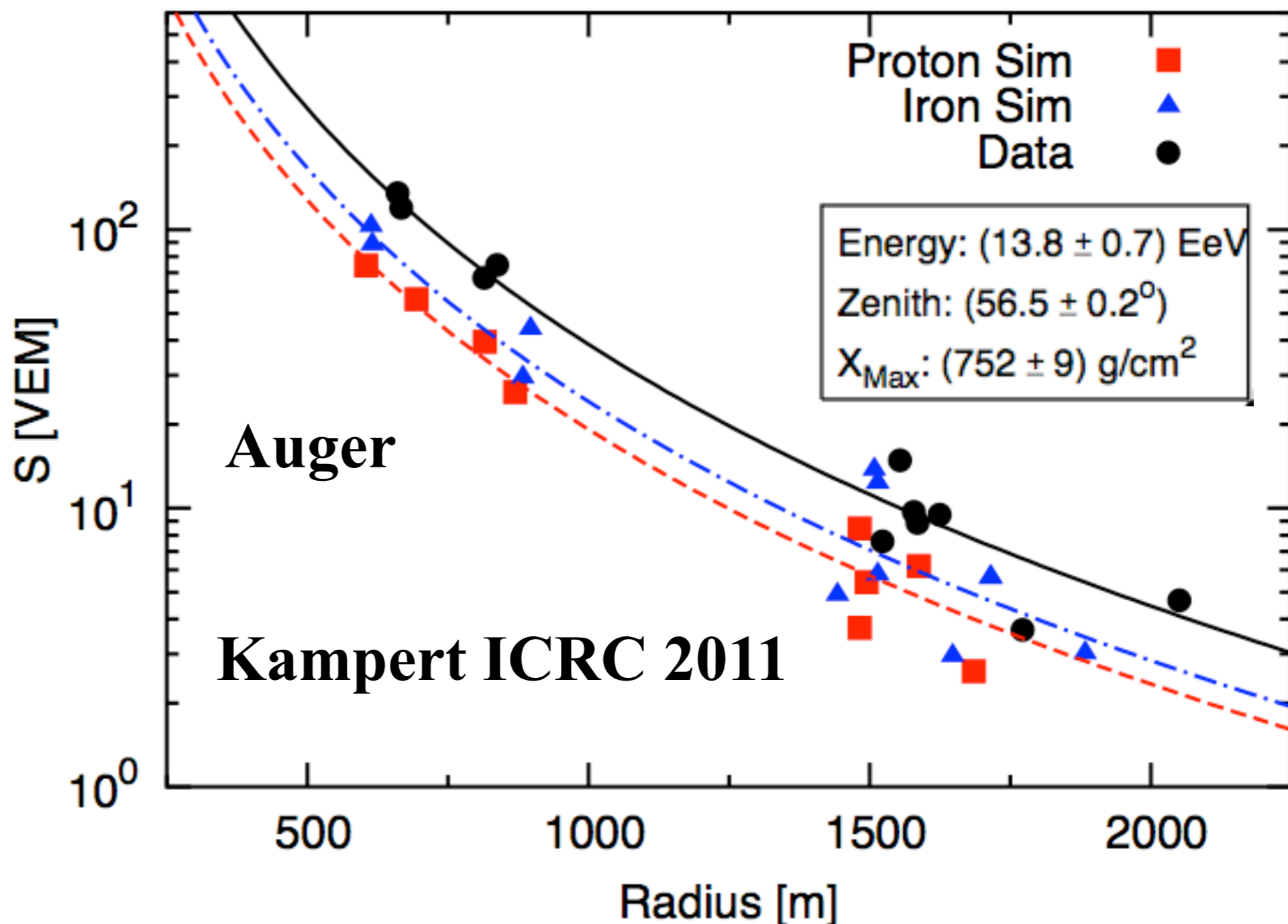
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Third SELFAS2 cross check with data :

Signal in Cerenkov tank VS distance to shower axis



Deficit of muons predicted by simulation with respect to signal observed in the Cerenkov tank in Auger data.

Scaling factor of ≈ 2

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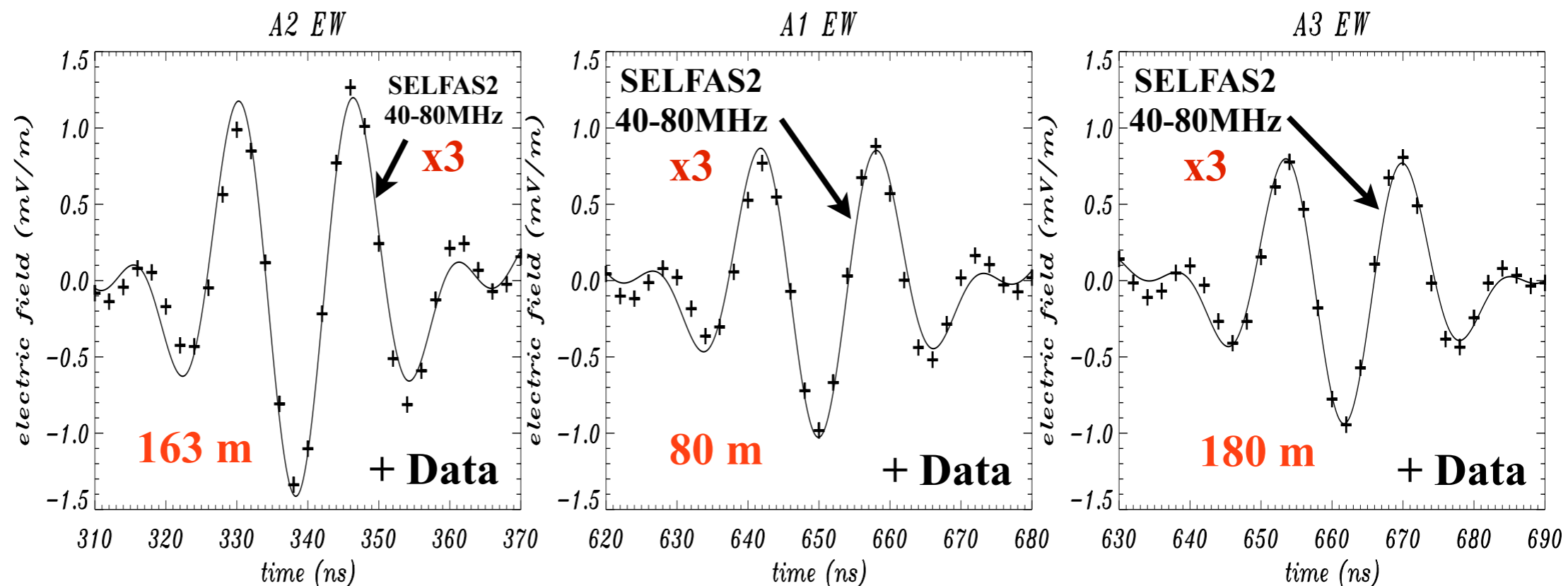
- SELFAS2 at RAuger1

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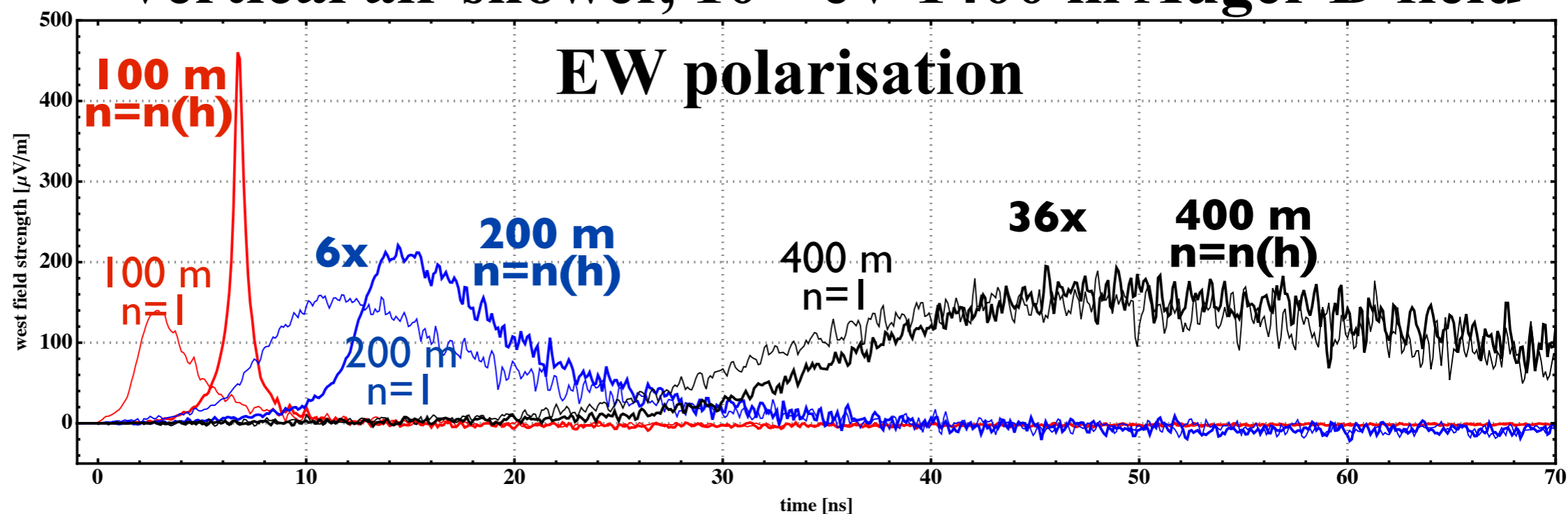
SELFAS2
with realistic air refractive index
 $n=n(h)$

SELFAS2

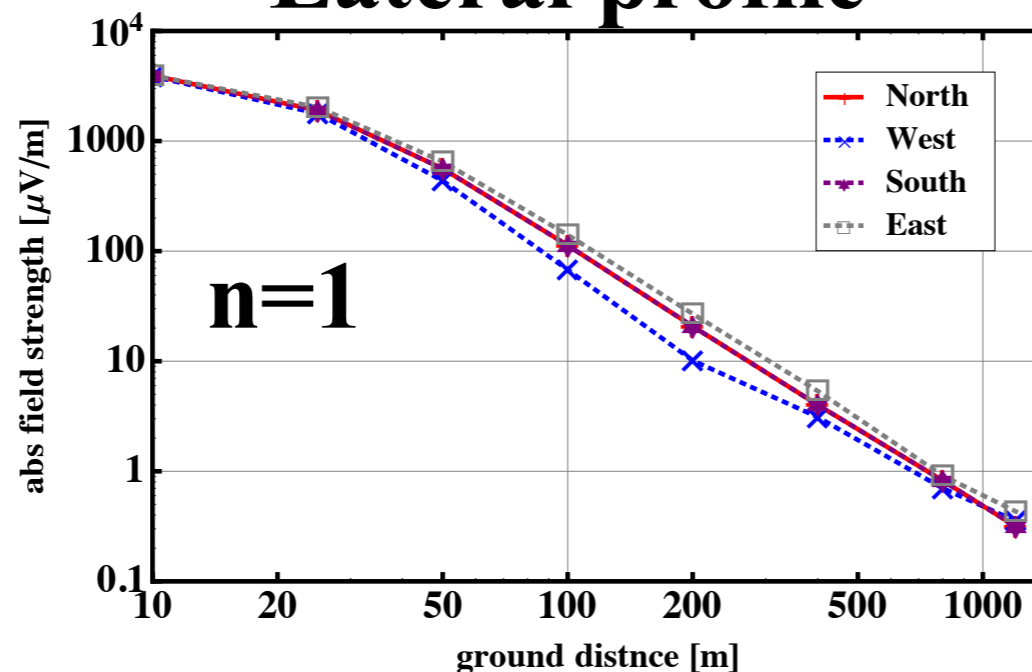
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SELFAS2 + realistic air refractive index

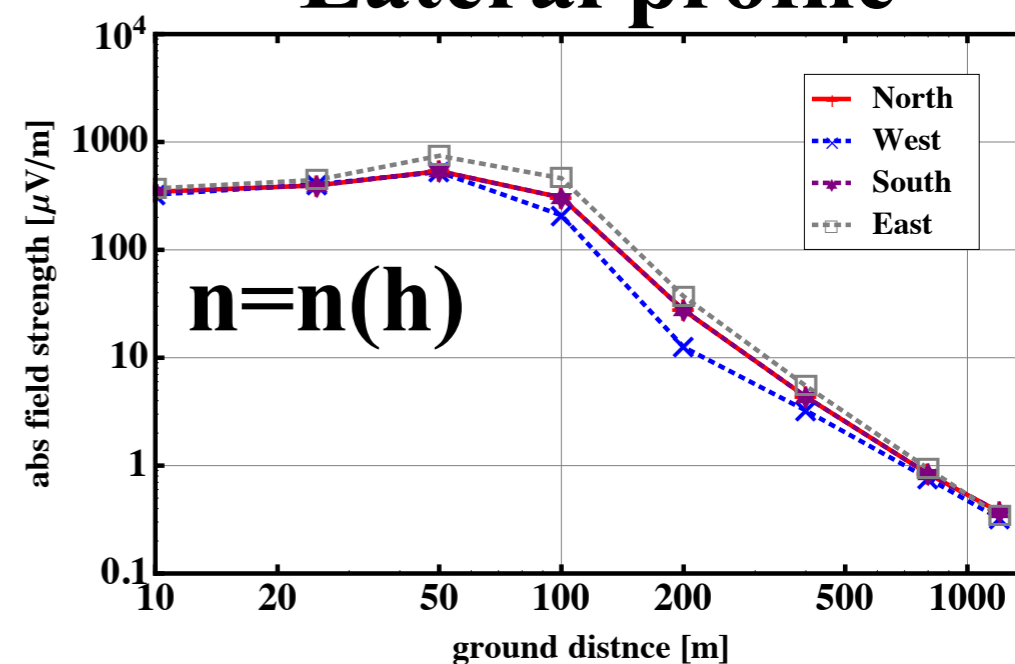
Vertical air shower, 10^{17} eV 1400 m Auger B-field



Lateral profile



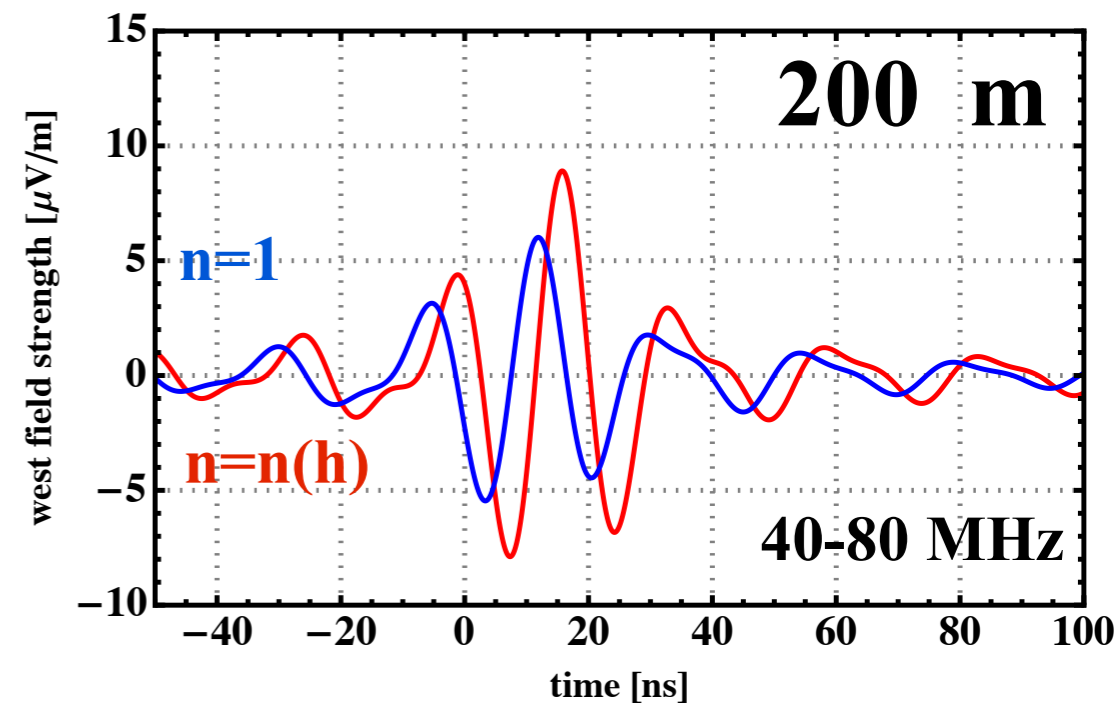
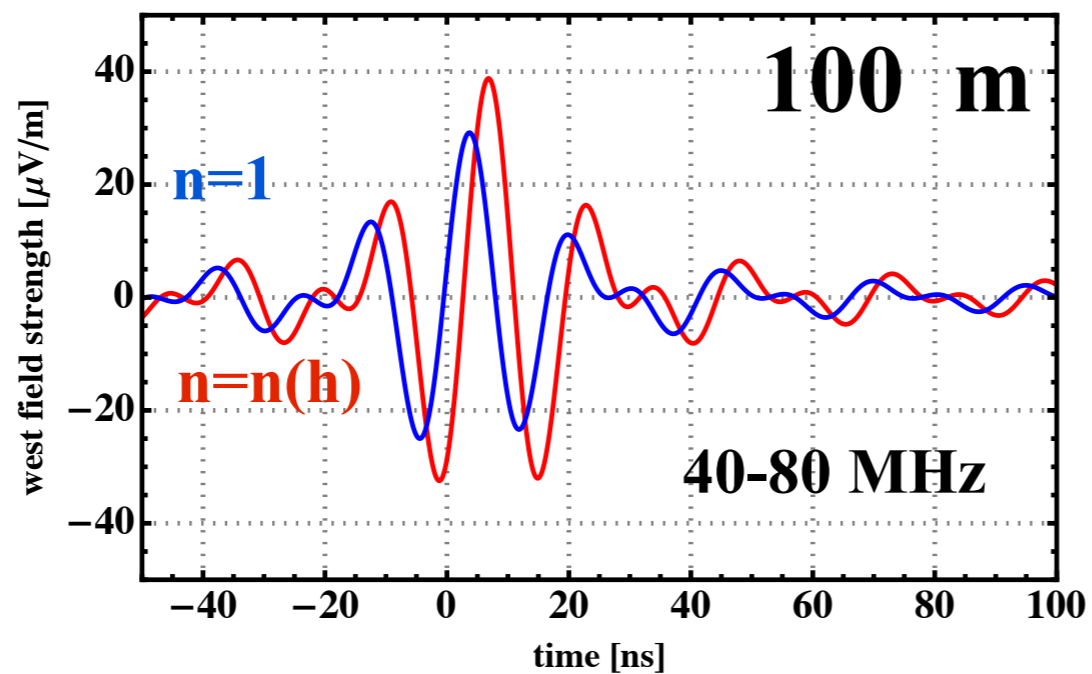
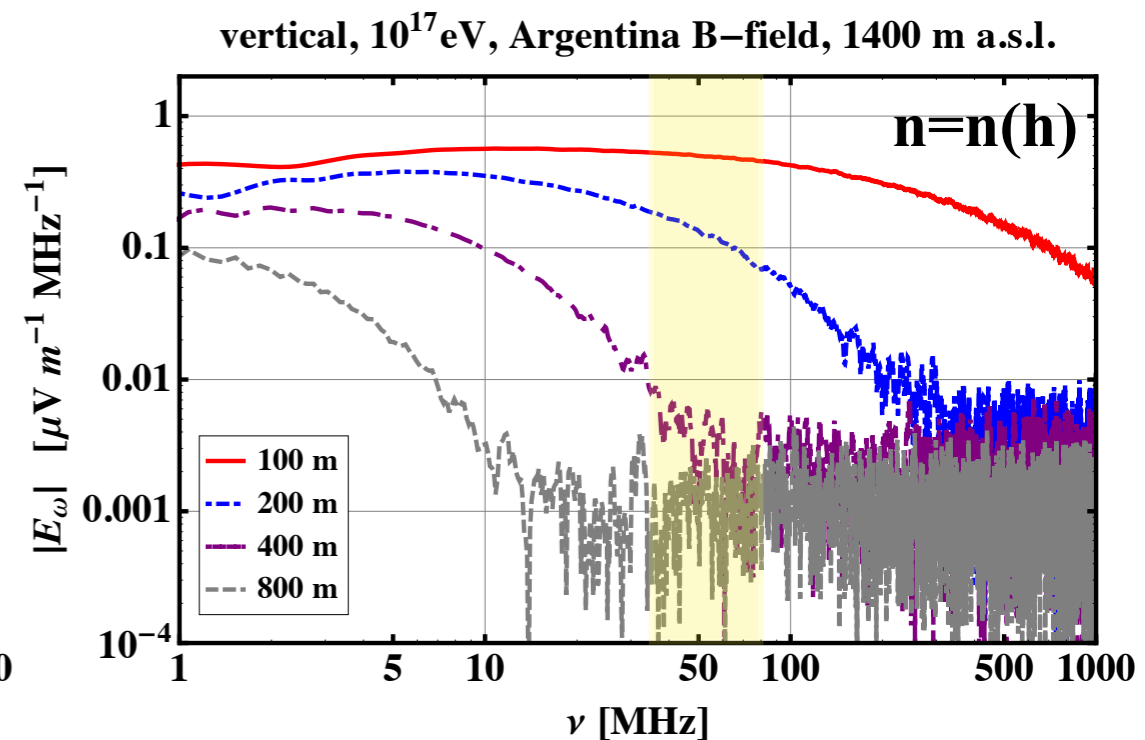
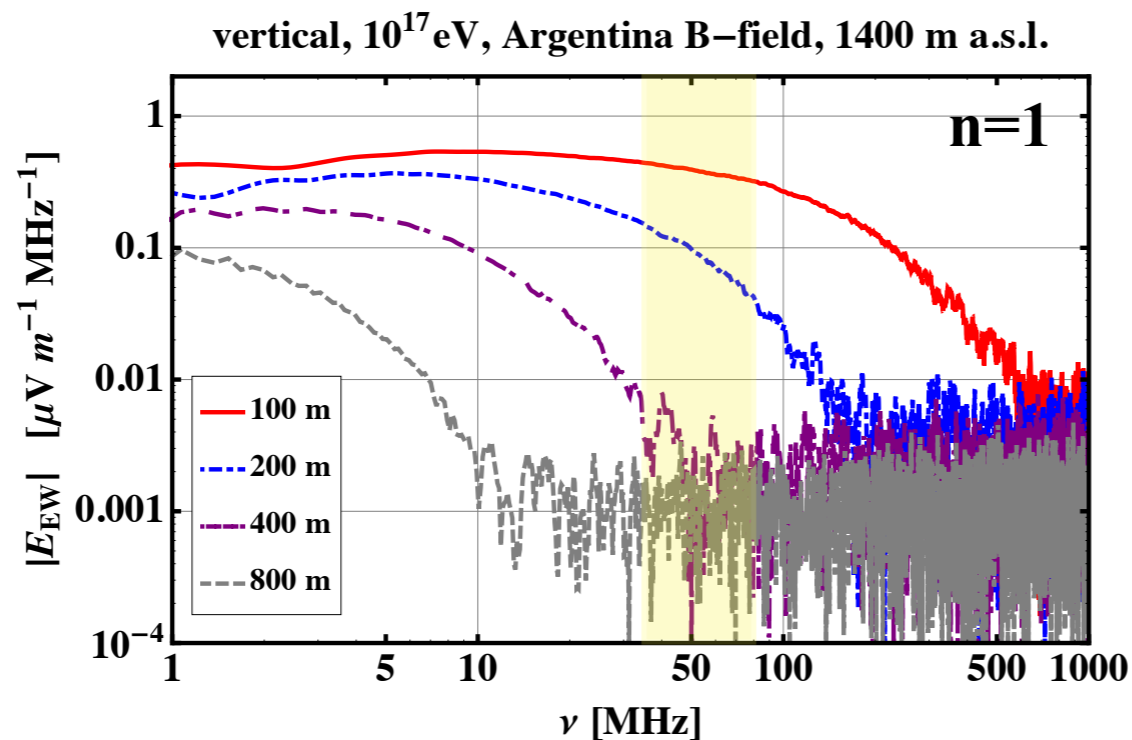
Lateral profile



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SELFAS2 + realistic air refractive index

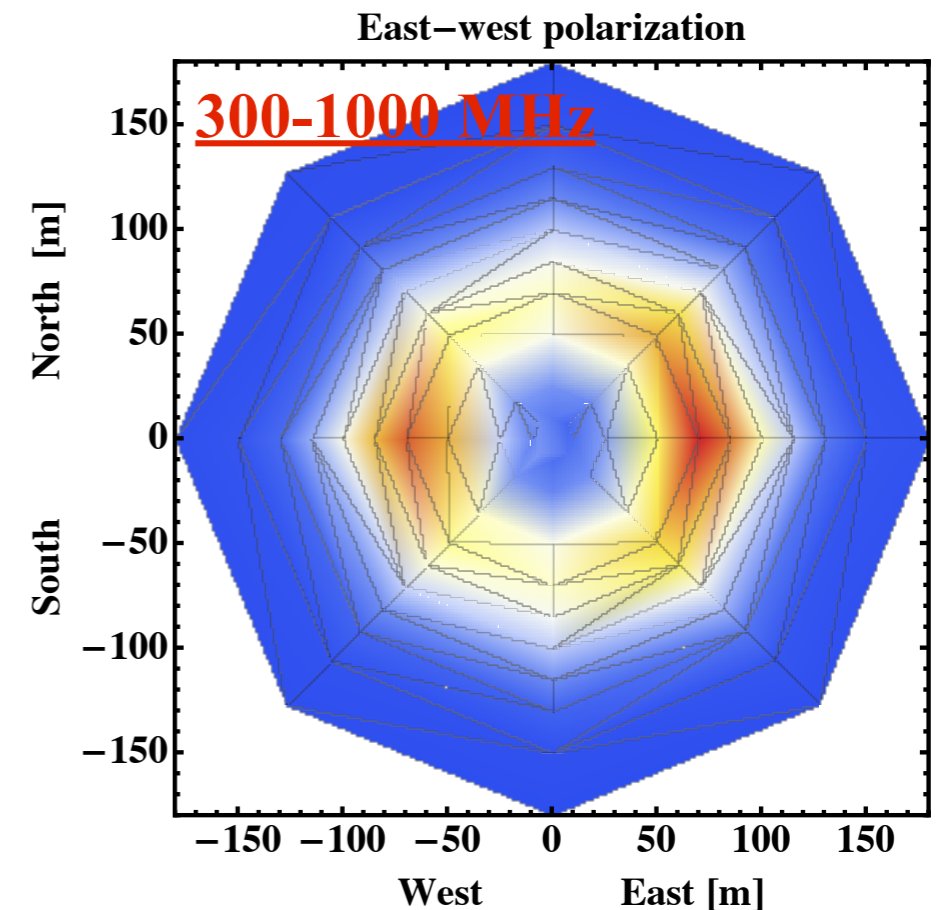
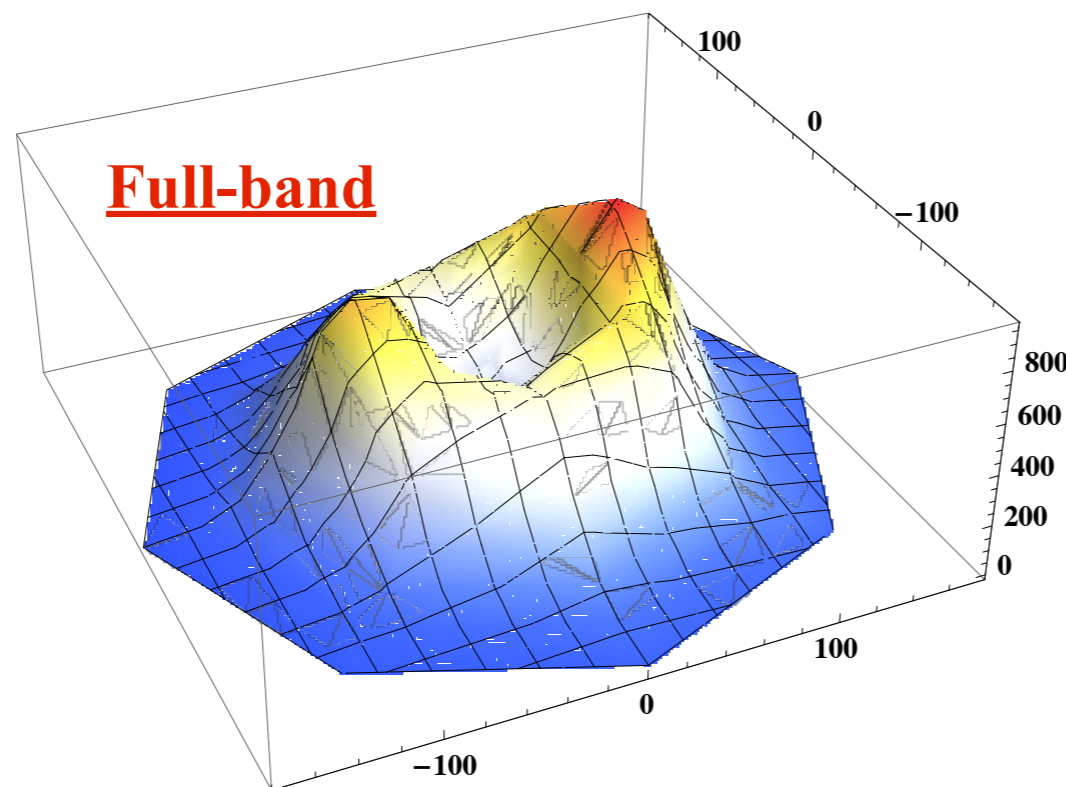
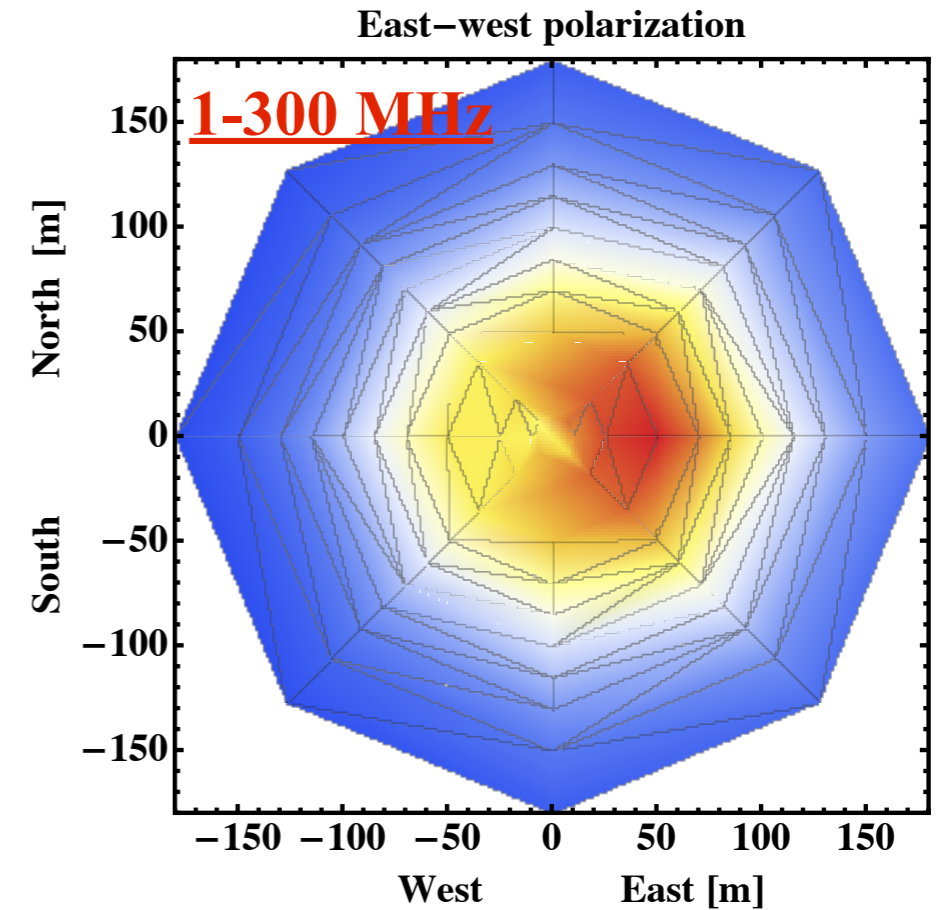
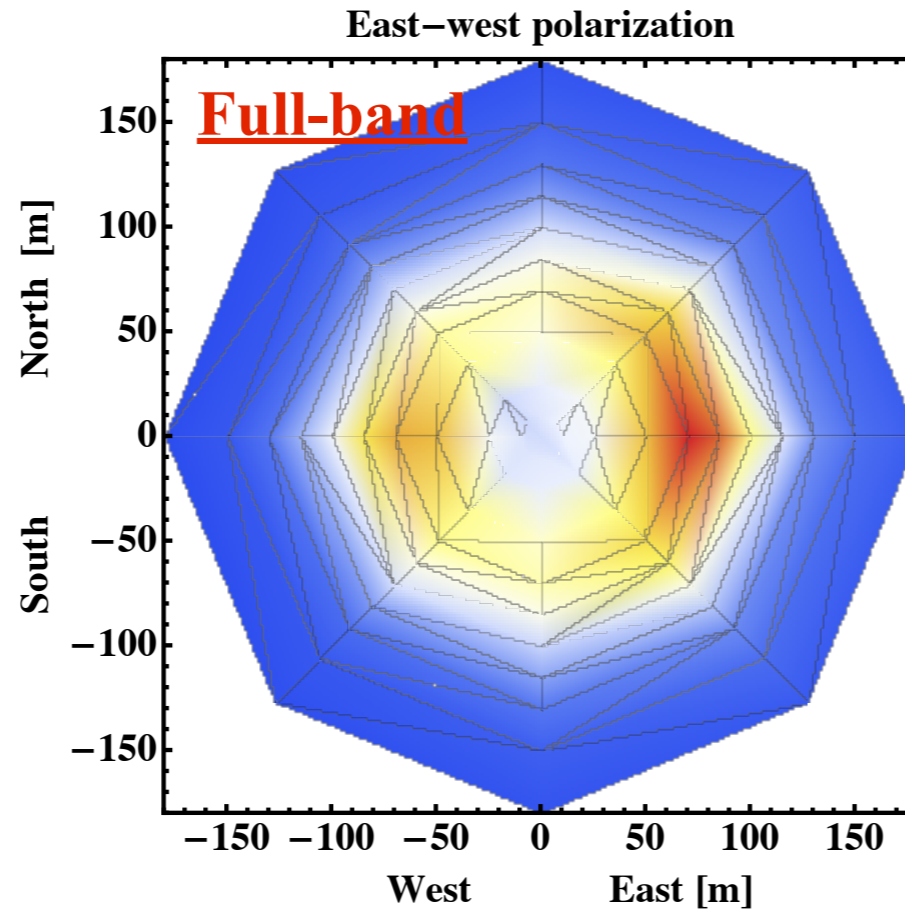


Realistic air refractive index **can not explain by itself** the scaling factor of 3 (**only 1.5**) observed between data and simulation in the 40-80 MHz

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- ➔ SELFAS is an autonomous Monte-Carlo simulation code based on universality
- ➔ SELFAS doesn't need EAS generator. The geometry only is needed.
- ➔ Microscopic radio-emission approach permits to take into consideration the complete air shower geometry (shower front thickness, lateral distribution)
- ➔ Typical computation time, recent mac book pro, 10^7 particles
 - one event, one antenna \approx **13 min**

SELFAS2 at Astroparticle Physics DOI : [10.1016/j.astropartphys.2012.03.007](https://doi.org/10.1016/j.astropartphys.2012.03.007)

- ➔ Comparison with data give promising results:
 - interpretation of the radio core shift in the CODALEMA data *Marin ICRC 2011 and currently under review in Astroparticle Physics*
 - reproduction of the CODALEMA skymap events
 - good agreement on the individual deconvoluted events
- ➔ But difference between predicted amplitude and data are not fully understood yet
- ➔ Realistic air refractive index is now implemented in SELFAS2

SELFAS2

Available freely at :

<https://sites.google.com/site/selfascode>

Tanks for attention...